

Vacancy thermodynamics and diffusion-controlled processes in intermetallics for functional and construction material technologies

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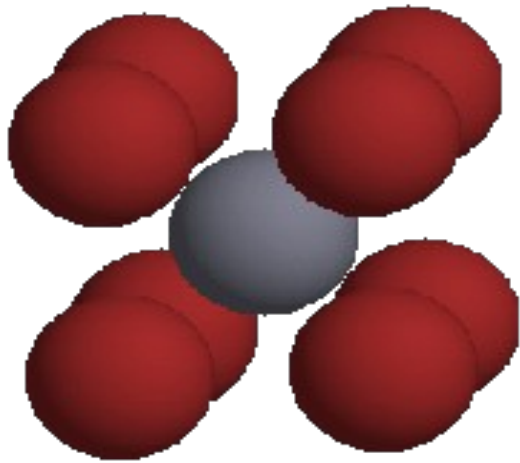
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JAGIELLONIAN
UNIVERSITY
IN KRAKOW

Recently studied systems

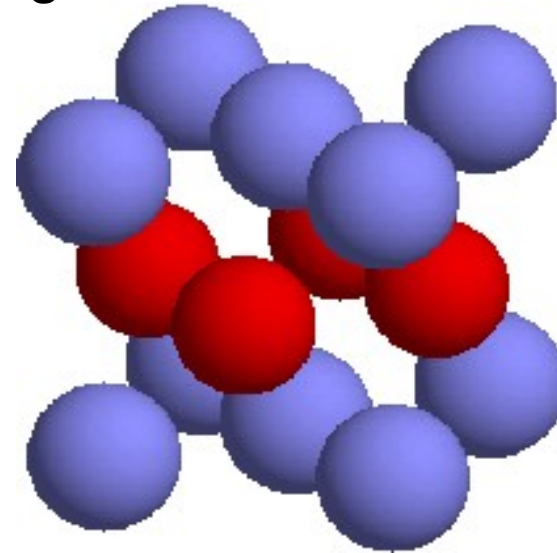
BCC-based **B2**
construction material



NiAl

Research by means of
modeling - A. Biborski

FCC-based **L1₂**
magnetic functional material

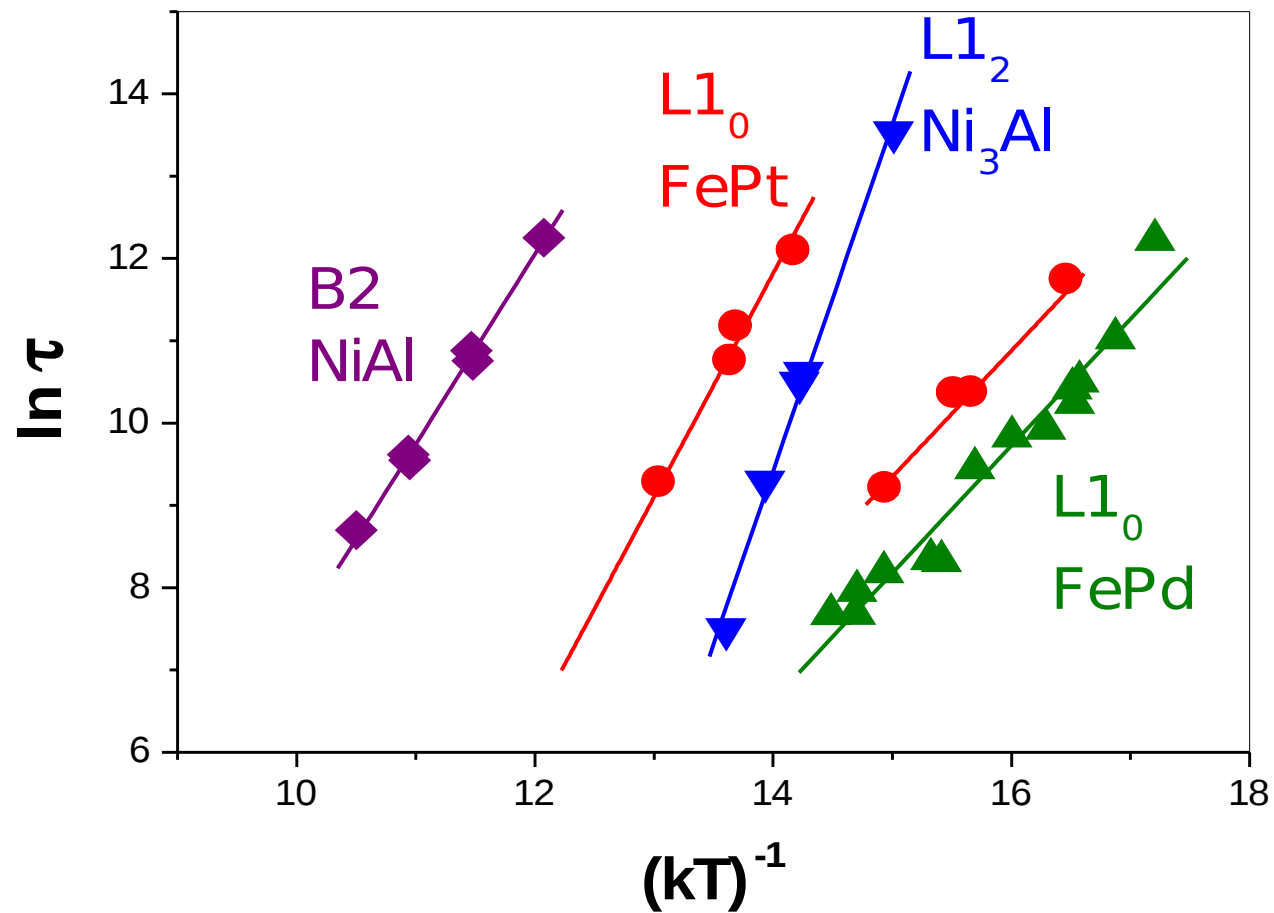


FePt

Research by means of
modeling - M. Kozlowski

General experimental and modeling research of
intermetallic systems carried out in group of
prof. R. Kozubski IF,UJ

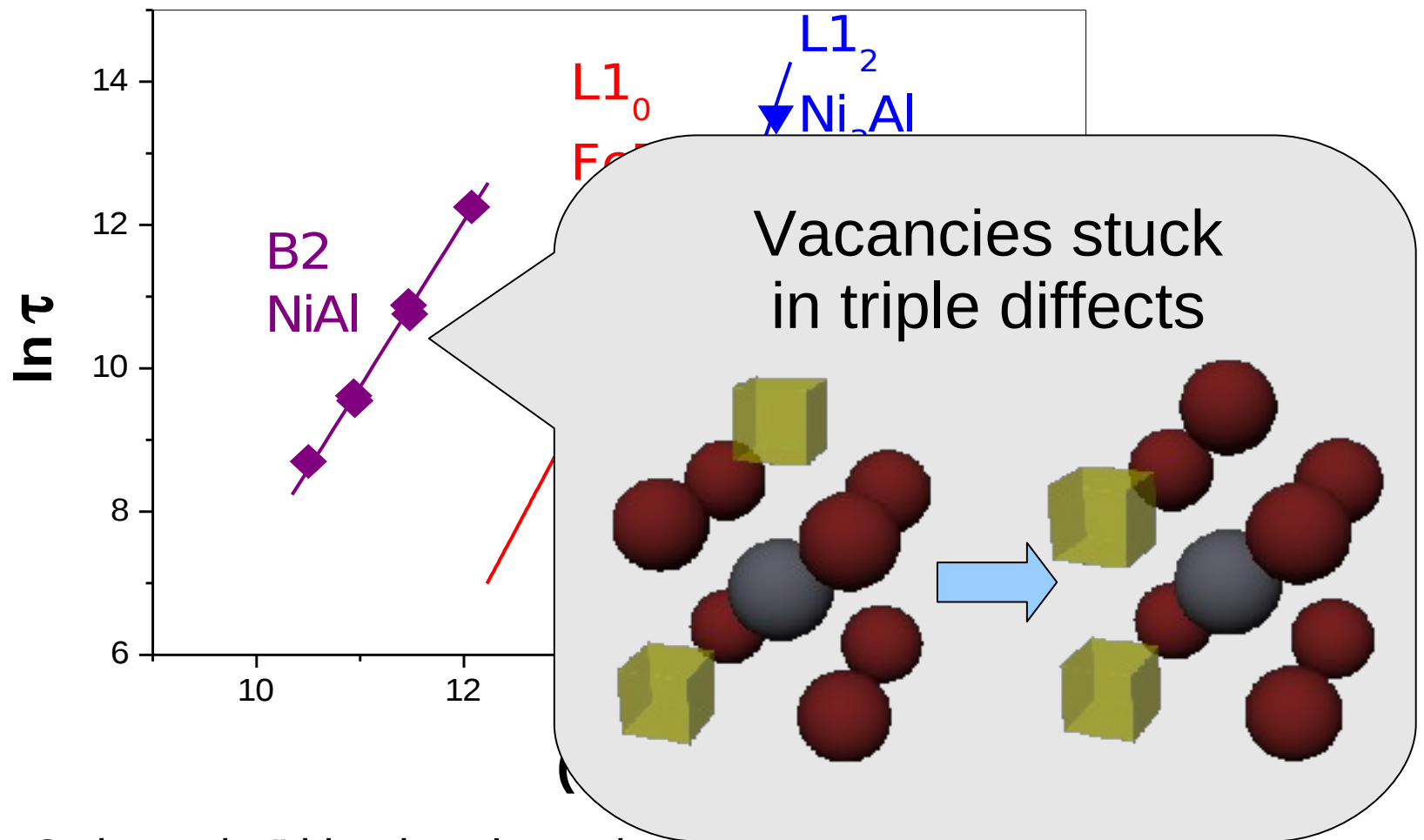
Phenomena studied in B2



„Order-order” kinetics slower in B2 NiAl than in L1₂ Ni₃Al
experimental observations (Kozubski et al.).

But equilibrium vacancy concentration being around 5 orders of
magnitude higher in B2 phase – up to $\sim 10^{-2}$ (Scheafer et al.)

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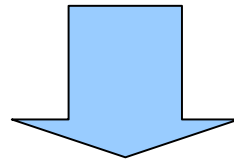
But equilibrium vacancy concentration being around 5 orders of
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B2 model approach

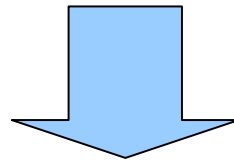


**Modeling of „order-order” kinetics
in triple-defect type B2 superstructure
at equilibrium vacancy concentration**

**Set model interatomic potentials
that promote triple defect**



**Determine chemical potentials that result
in equilibrium vacancy concentration**



**„Order-order” kinetics
via vacancy mechanism**

B2 model approach



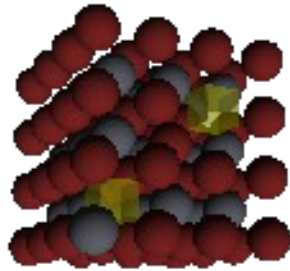
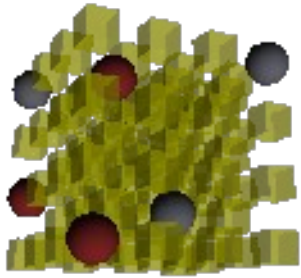
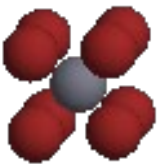
**Set model interatomic potentials
that promote triple defect**

**Selected pair-wise interactions promoting
triple-defect behaviour:**

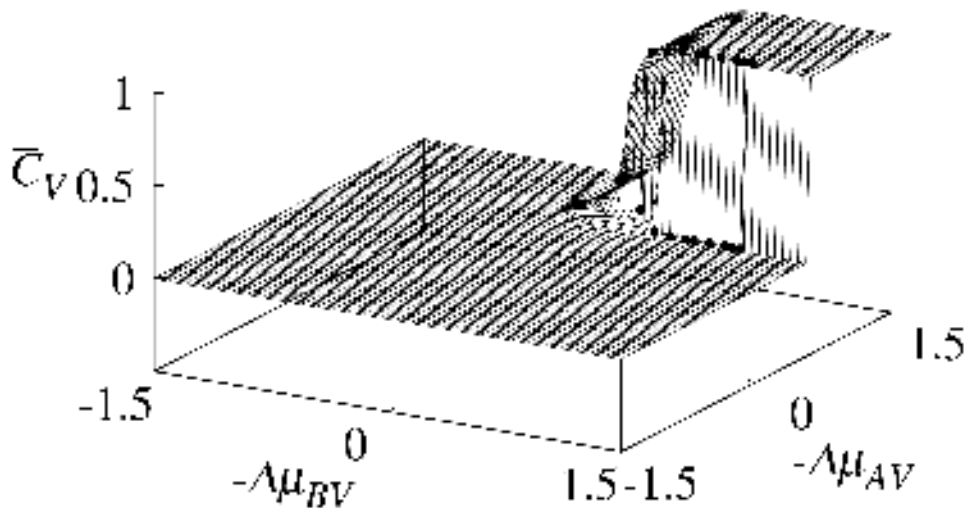
$$V_{AB} = -0.125 \quad V_{AA} = -0.120 \quad V_{BB} = -0.050 \quad [eV]$$

$$V_{VV} = -0.000 \quad V_{AV} = 0.040 \quad V_{BB} = -0.040 \quad [eV]$$

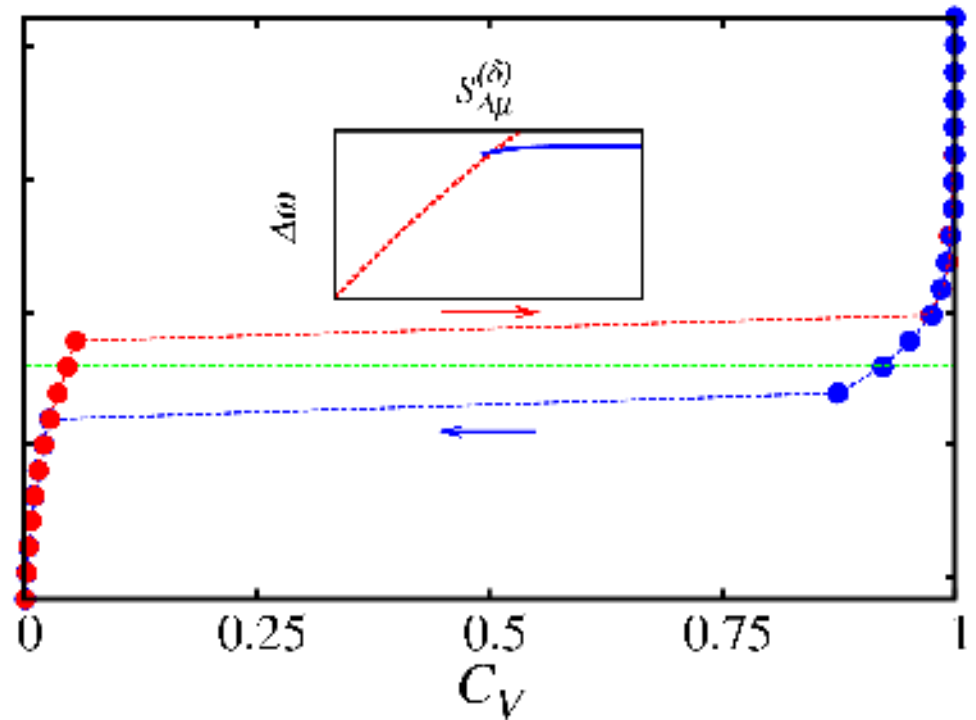
Lattice-gas decomposition SGCMC simulations



Desired system presents
co-existence of phases

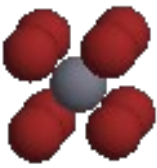


$S_{\Delta\mu}^{(\delta)}$

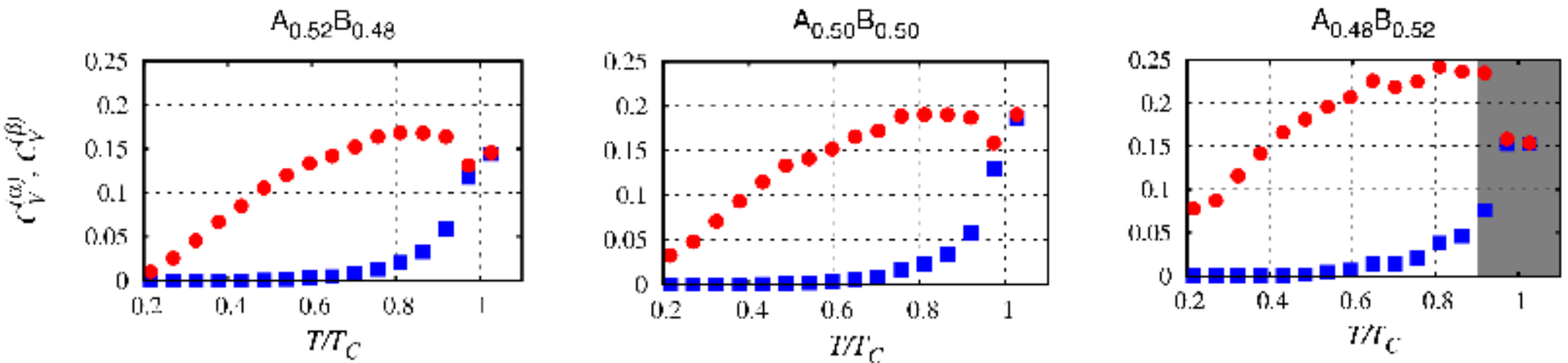


**Refining procedures
performed successfully
resulting in equilibrium
thermal vacancy concentration
as a function of temperature**

Lattice-gas decomposition SGCMC simulations



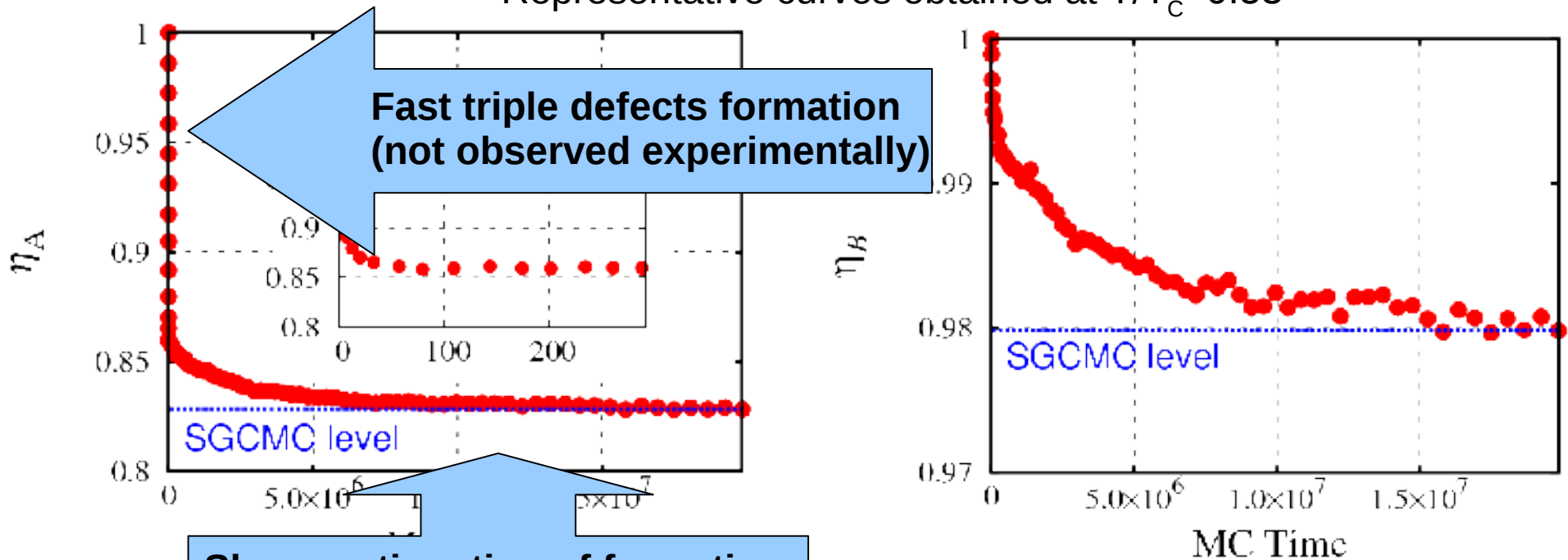
Atom-rich solution (crystal at thermal and chemical equilibrium)



„Order-order” kinetics Kinetic Monte-Carlo simulations



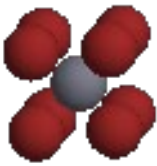
Representative curves obtained at $T/T_c=0.53$



Fast triple defects formation
(not observed experimentally)

Slow continuation of formation
of A-atom antisites
(observed experimentally)

LRO evolution



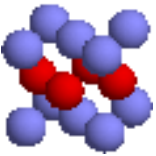
B2 model - conclusion

SGCMC with **phase decomposition procedure** is the successful method for determination of **equilibrium vacancy concentration** in binary systems.

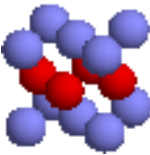
It is possible to adjust energies in the system to generate **triple-defect** and observe “**order-order**” **kinetics** similar to the **experimental**

Perspective – use realistic potentials and generate quantitative agreement with experiment.

Atomic ordering in $L1_0$ FePt thin layers



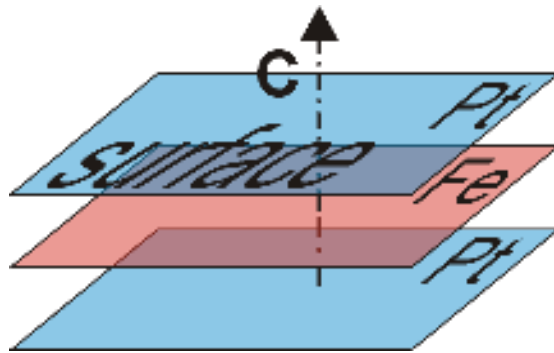
L1₀ FePt layers – basic concepts



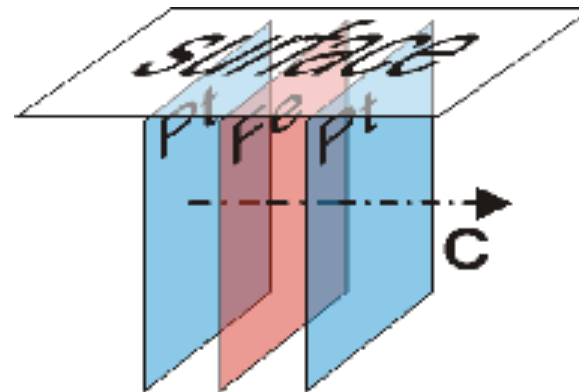
Two models:

ISING-type – discrete pair interactions based on CEM
ABOP – advanced many-body interactions MD-like

Superstructure variants:

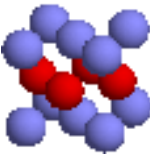


c-variant



a(b)-variant

ISING model Monte Carlo simulations

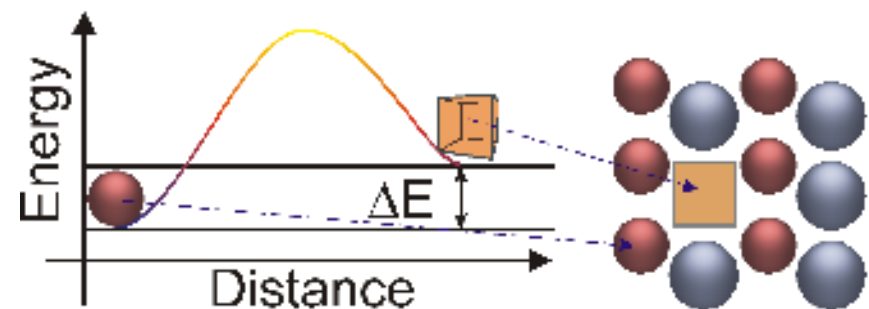


- **Ising** system with pair interaction energies up to the second nearest neighbour.

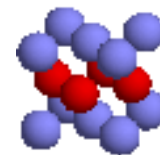
$$E_{Conf} = \sum_{i,j,r} N_{ij} V_{ij}(r)$$

- Potentials developed CEM (Cluster Expansion Method)
- Atomic migration simulated by **jumps to nn vacancies** with probabilities determined within **Glauber** dynamics.

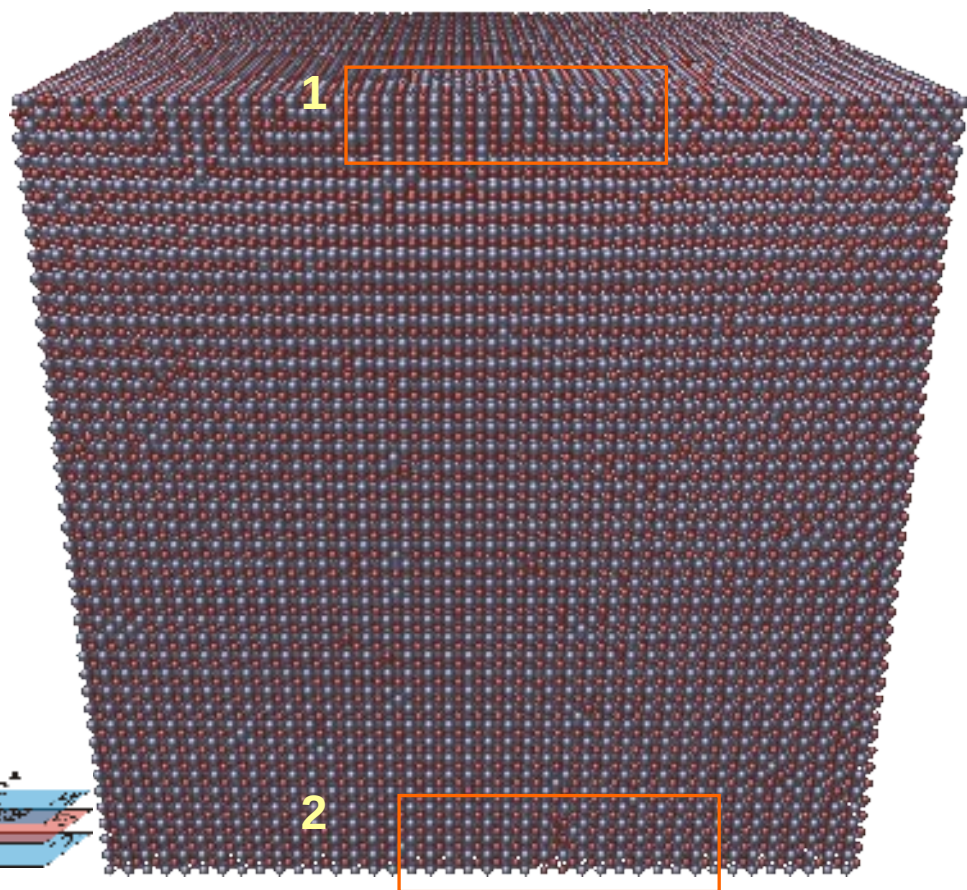
$$P_{i \rightarrow j} = \frac{\exp\left(-\frac{\Delta E}{k_B T}\right)}{1 + \exp\left(-\frac{\Delta E}{k_B T}\right)}$$



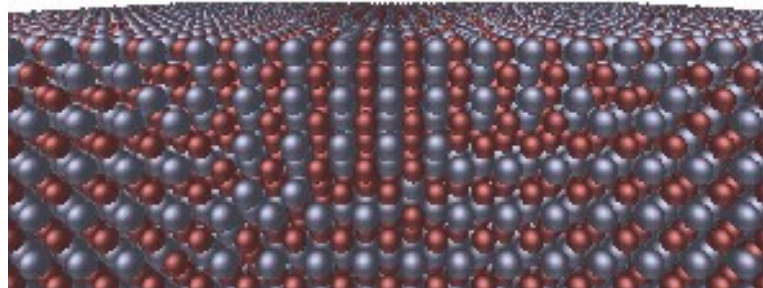
ISING model - L1₀ FePt c-variant layers



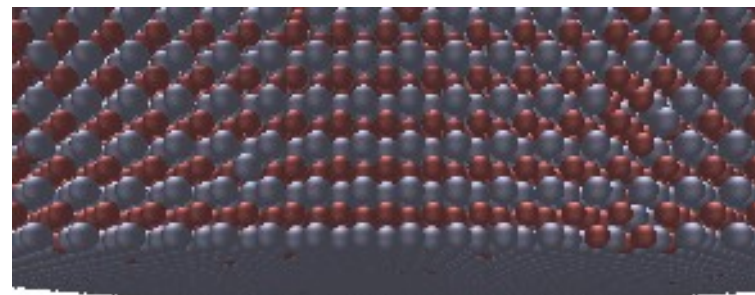
FePt L1₀ c-variant → a-variant superstructure reorientation



1 Fe-covered surface



2

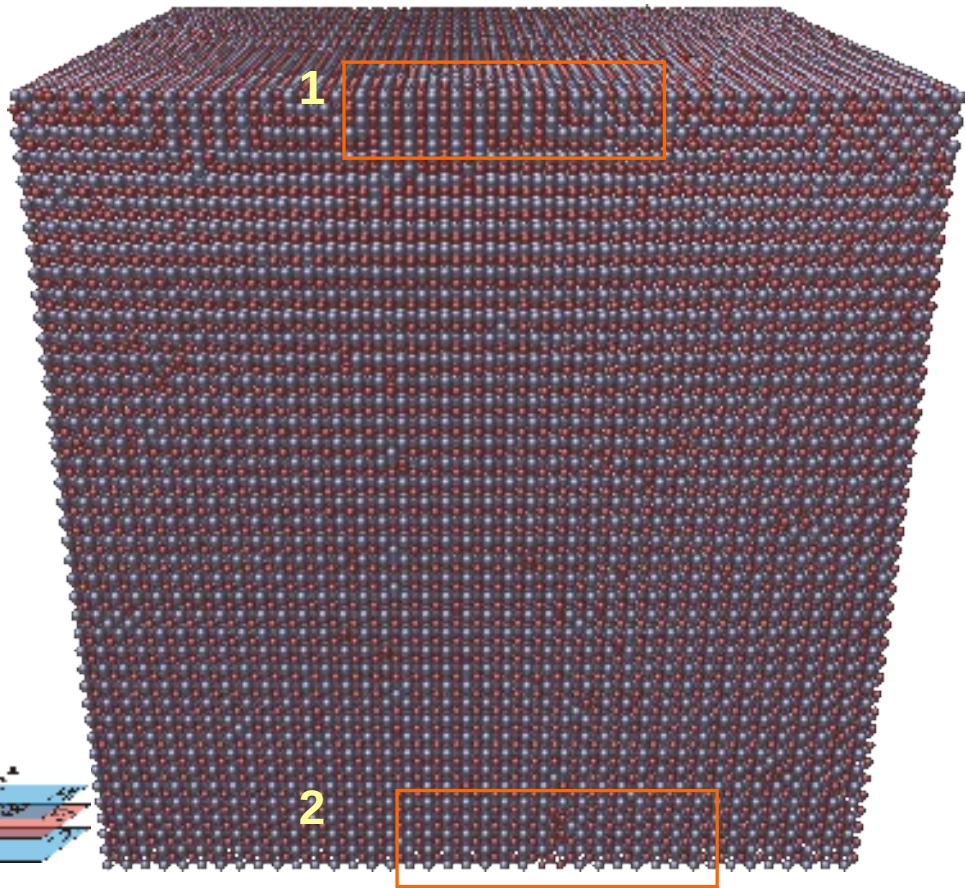
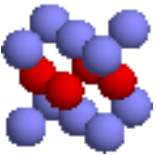


Pt-covered surface

Simulated L1₀ FePt c-variant layer
after 5x10⁷ MC steps at T = 1000K

● - Fe, ● - Pt, □ - vacancy.

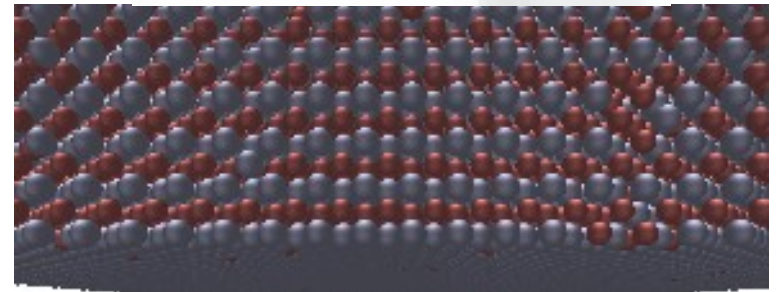
ISING model - L1₀ FePt c-variant layers



1 Fe-covered surface



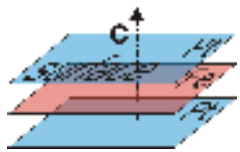
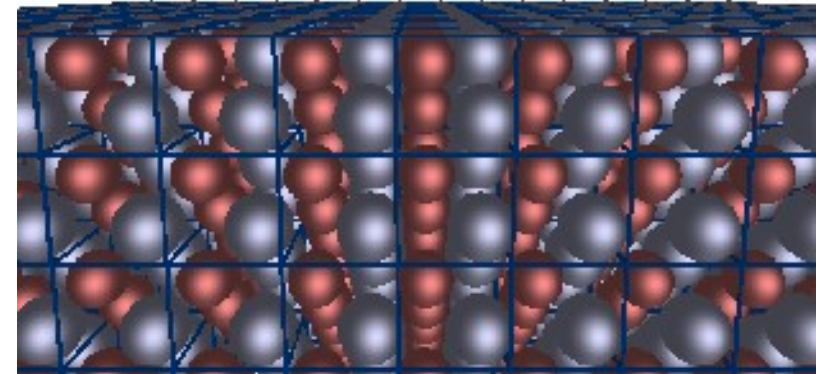
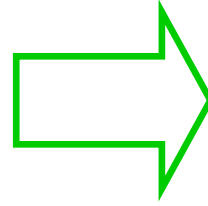
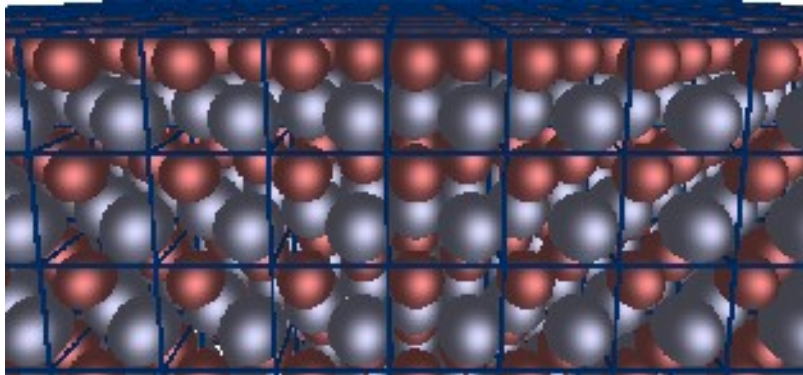
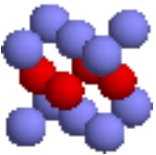
2



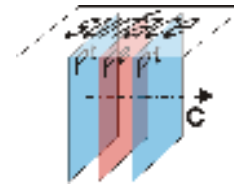
Pt-covered surface



Energetic instability



c-variant
c \perp surface



a(b)-variant
c \parallel surface

$$\Delta E_{uc} = 2V_{FePt} - V_{FeFe} - V_{PtPt} < 0$$



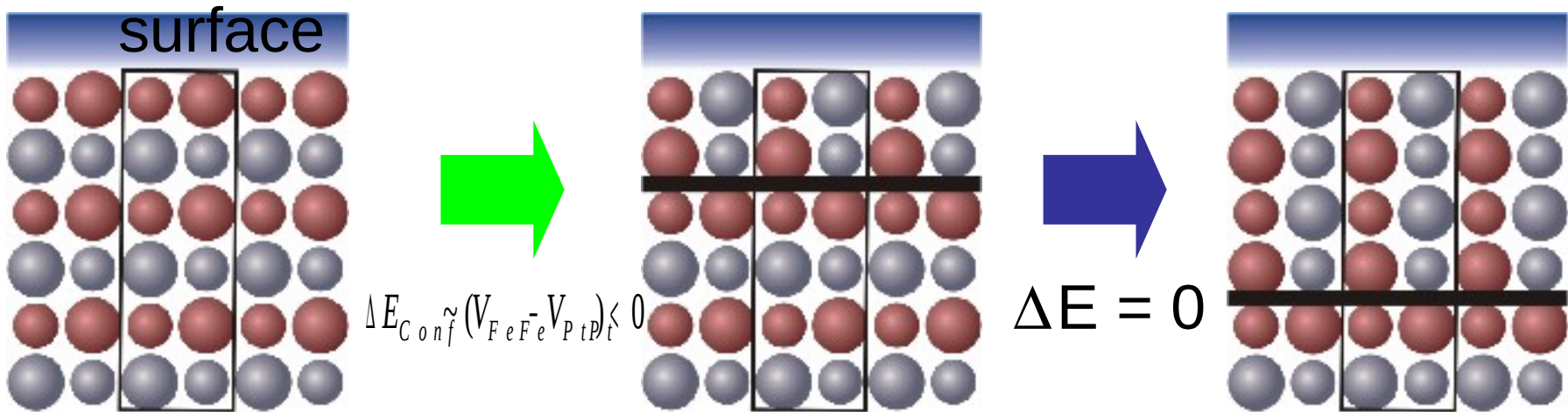
- FePt L1₀ unit cell



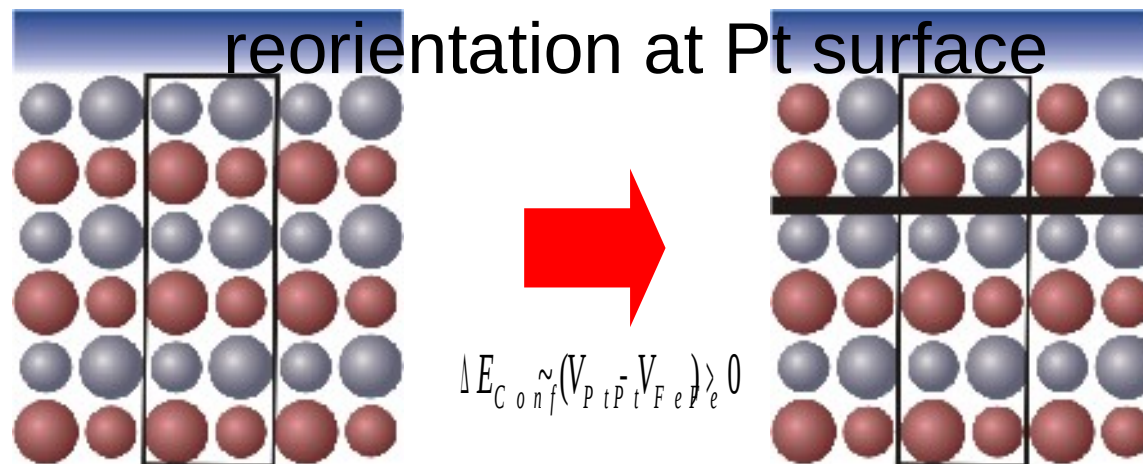
Driving force

Energetically **favorable**
reorientation at **Fe**

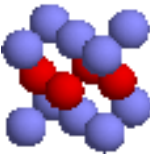
No energy **change** during
domain **growth**



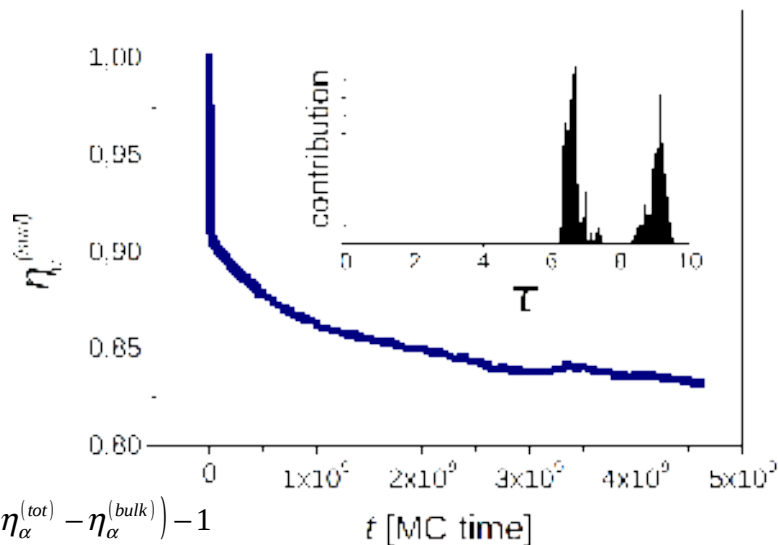
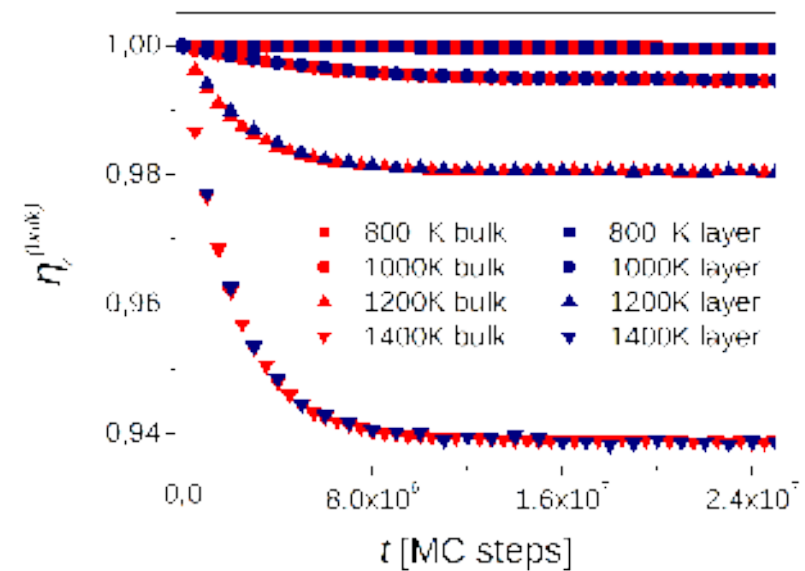
Energetically unfavorable

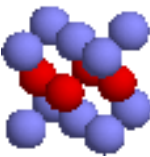


Reorientation kinetics



0. homogeneous disordering (generation of antisite defects).
1. nucleation of a- and b-variant $L1_0$ domains within the surface layer of the $L1_0$ unit cells
2. growth of the nucleated a- and b-variant $L1_0$ domains inward the layer
3. relaxation of the microstructure of a- and b-variant $L1_0$ domains



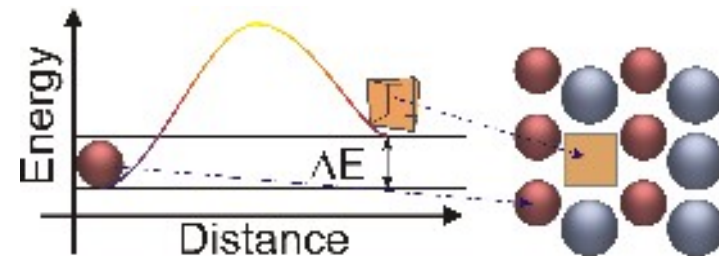


ABOP – MC/SR simulations

Monte Carlo / Static Relaxations (MS + Lattice optimization)

MC – atomic migrations by means of Glauber algorithm.

$$P_{i \rightarrow j} = \frac{\exp\left(-\frac{\Delta E}{k_B T}\right)}{1 + \exp\left(-\frac{\Delta E}{k_B T}\right)}$$

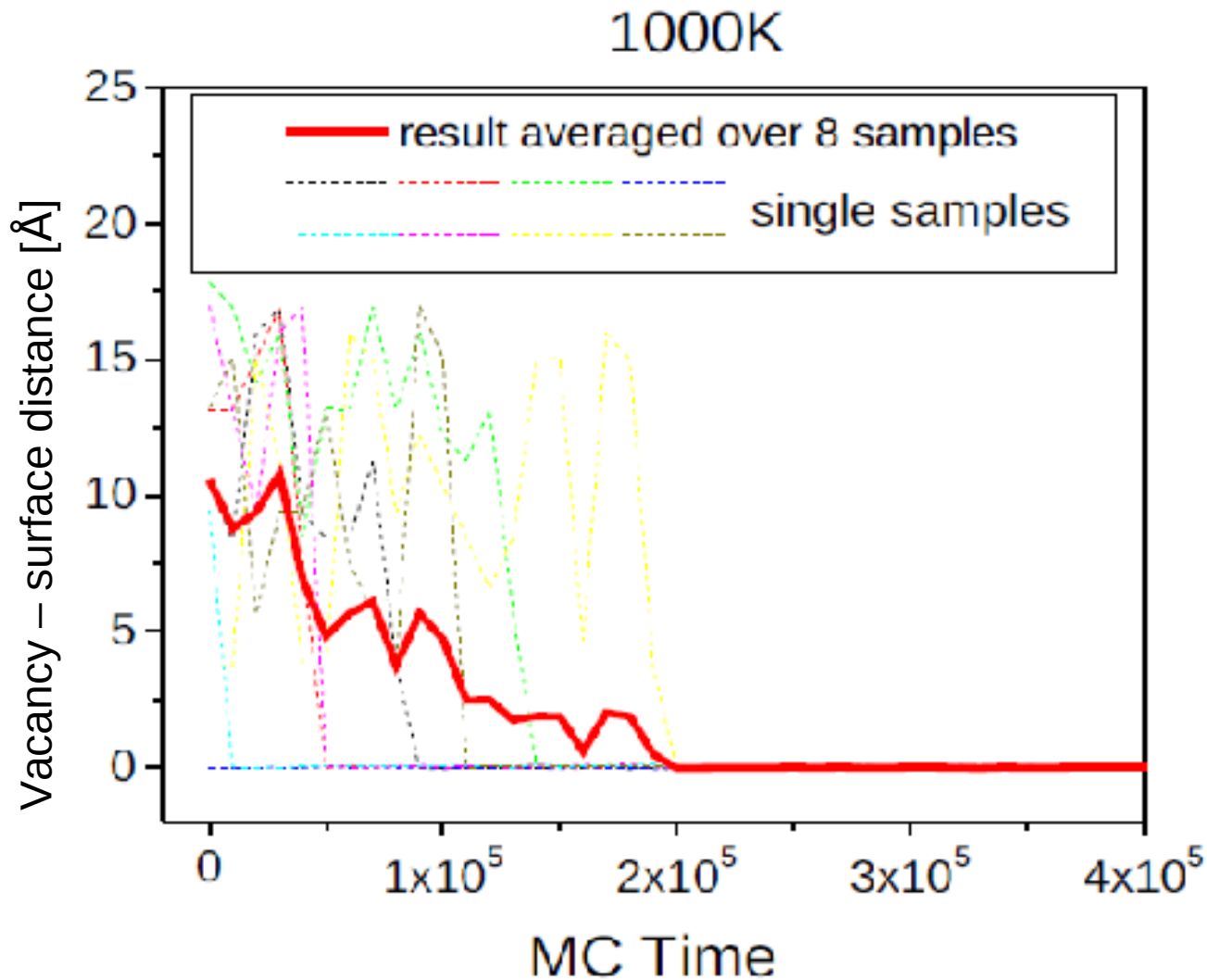
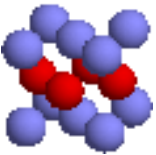


MS – molecular statics for surface relaxations

$$E = \sum_{i < j} f_{ij}^c(r_{ij}) \left[V_{ij}^R(r_{ij}) - \frac{b_{ij} + b_{ji}}{2} V_{ij}^A(r_{ij}) \right]$$

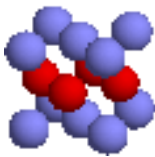
Lattice optimization – evolution of tetragonal distortion

ABOP model results – FePt L1₀ layers

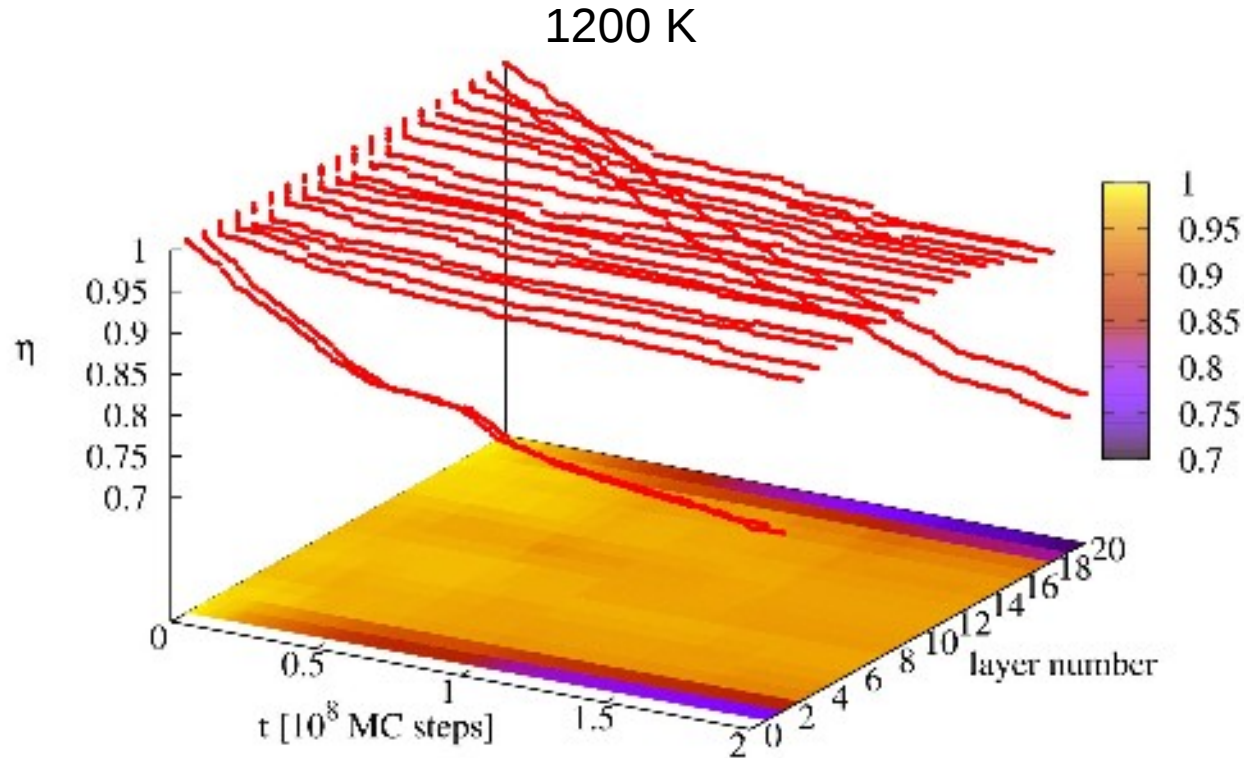


Vacancies stay at the surface

ABOP model FePt c-variant L1₀ layers



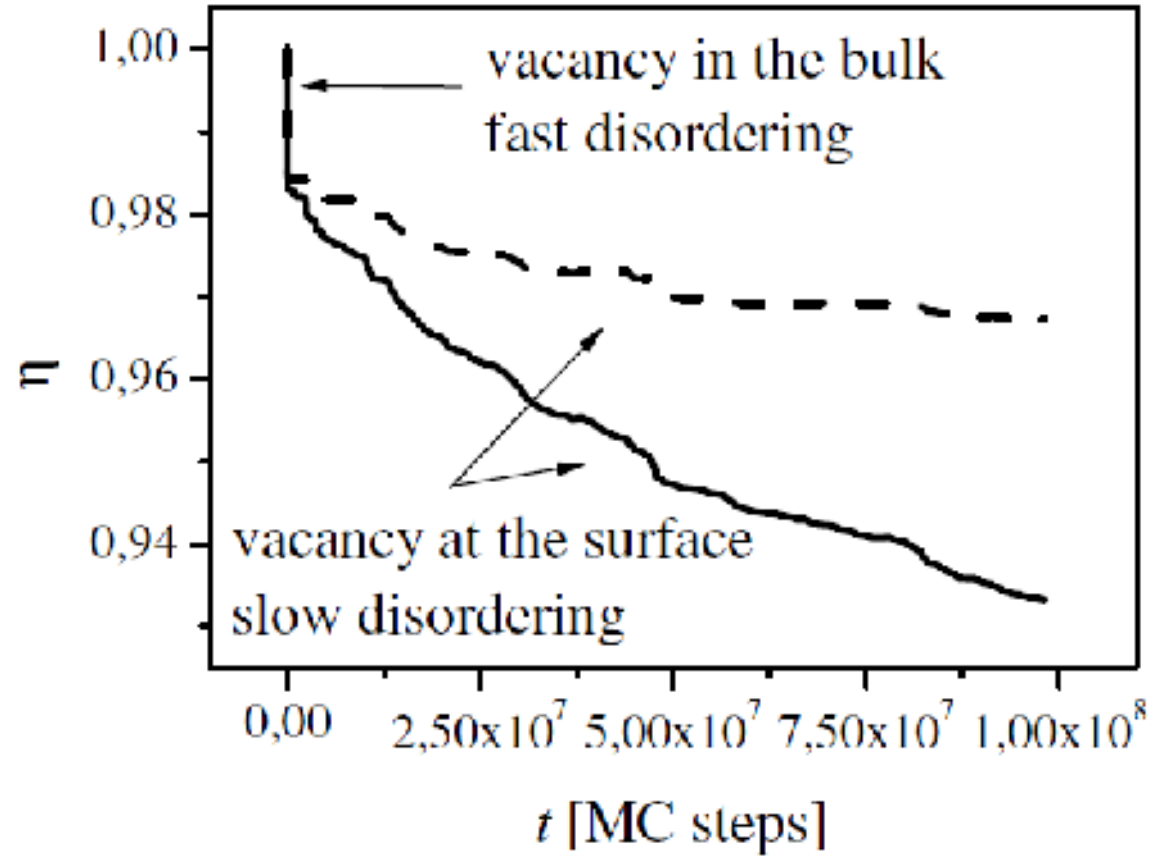
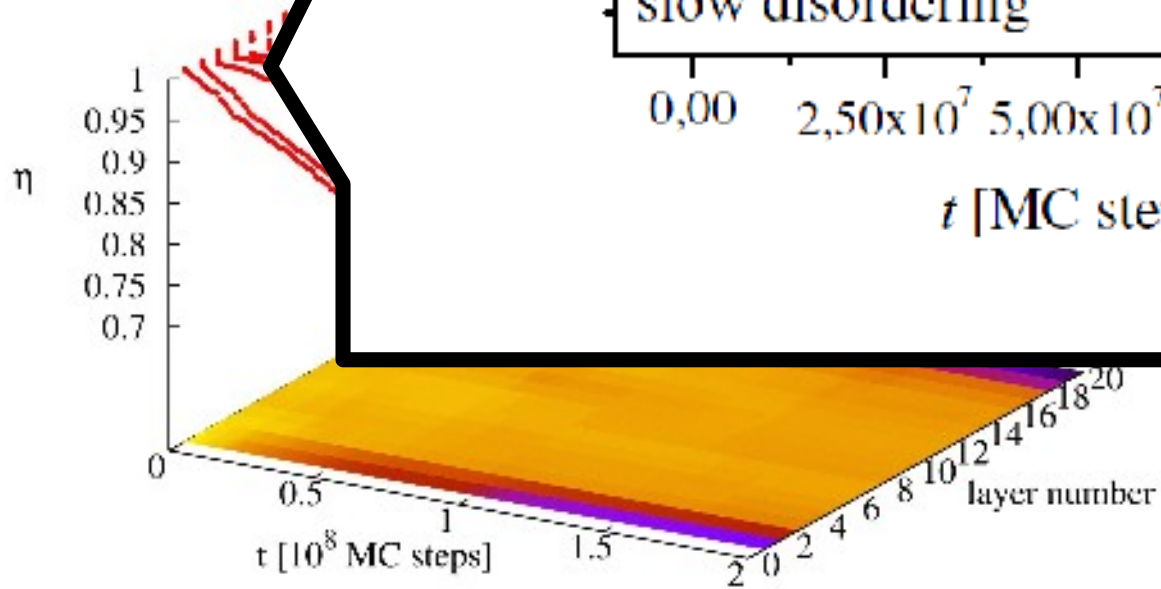
Samples 10x10x10 unit cells, initially c-variant L1₀, 1 vacancy.
Isothermal simulation. Results averaged over 8 runs



Metastable superstructure – localized surface disordering

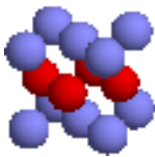
ABOP model

Samples 10x10x10 u
Isothermal simulation.

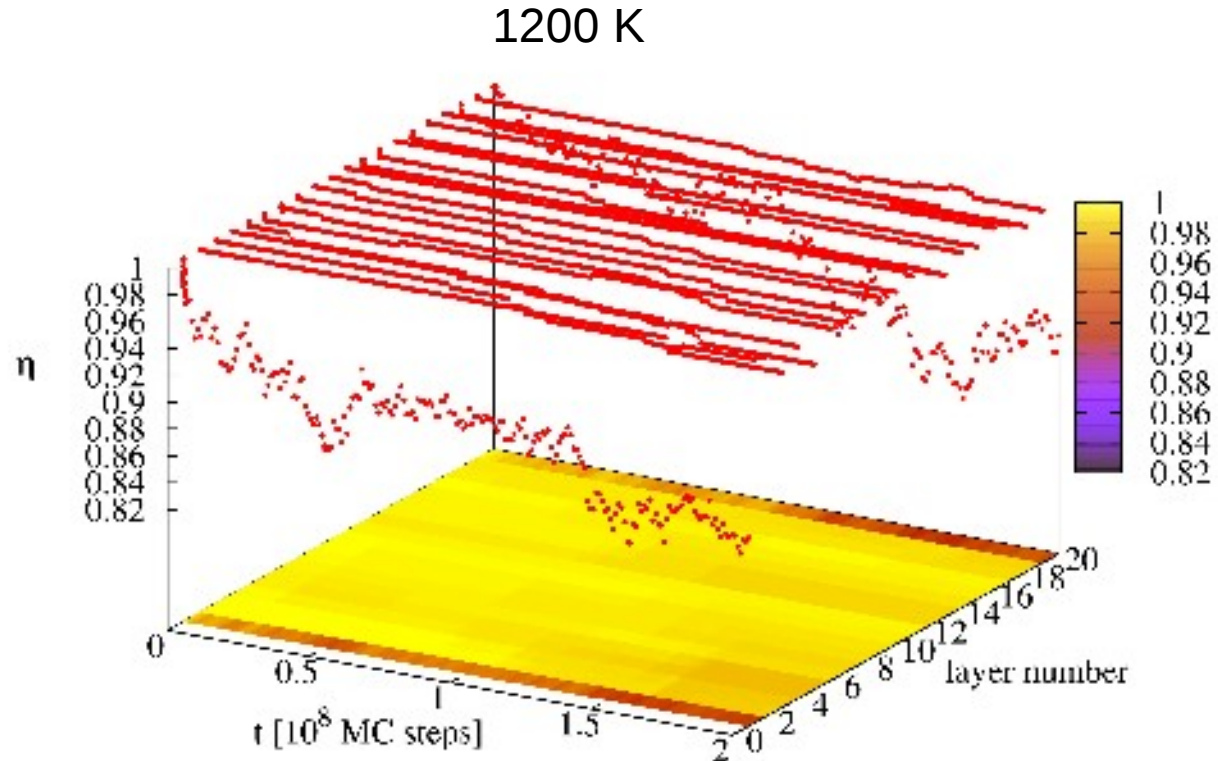


Metastable superstructure – localized surface disordering

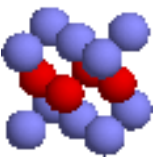
ABOP model FePt a-variant L1₀ layers



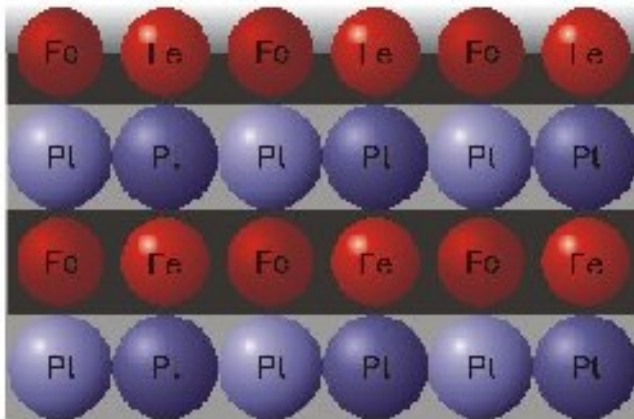
Samples 10x10x10 unit cells, initially a-variant L1₀, 1 vacancy.
Isothermal simulation. Results averaged over 8 runs



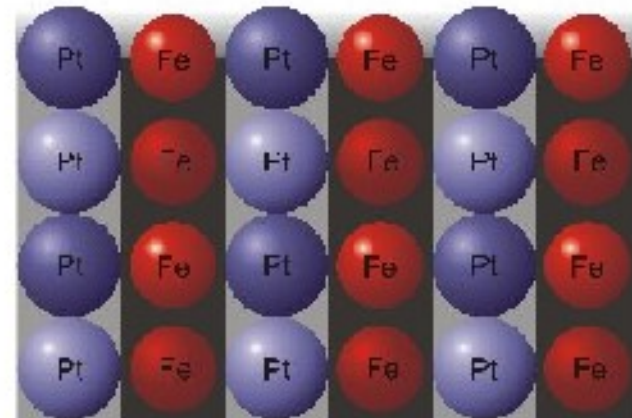
Stastable superstructure – localized surface disordering



L1₀ FePt layers summary I



c-variant

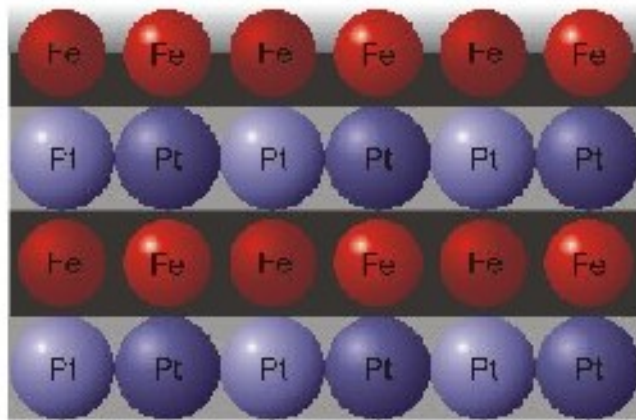
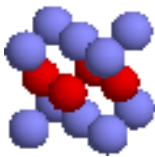


a-variant

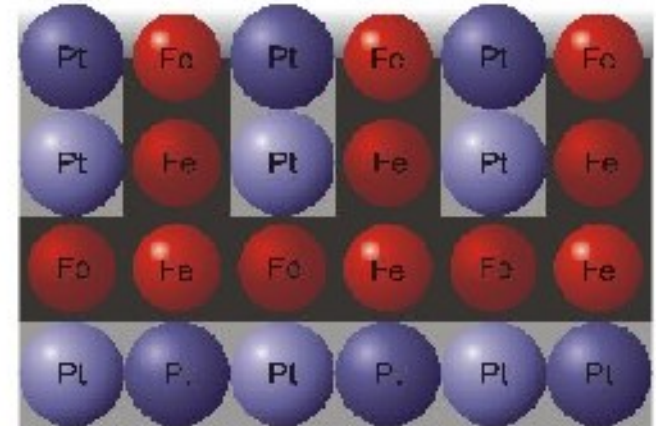
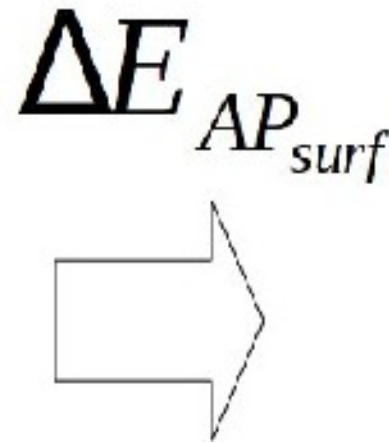
$$E_c > E_a$$

In all considered models configurational energy of c-variant L1₀ ordered FePt layer is lower than in a-variant layer.

L1₀ FePt layers summary II



c-variant



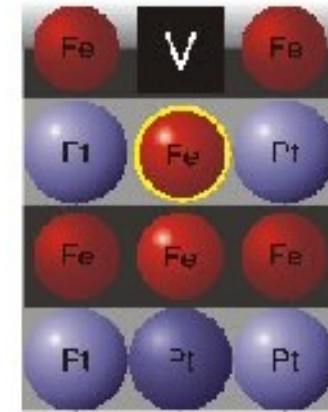
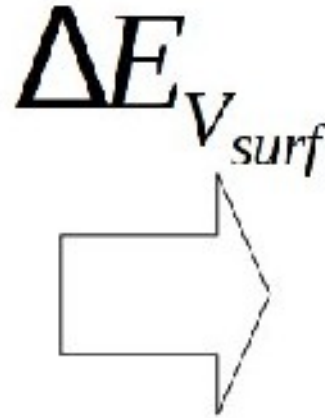
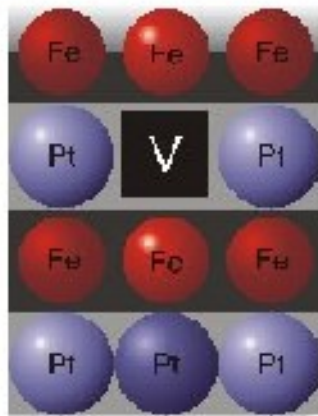
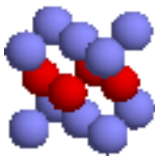
a-variant
at the surface of
c-variant

ISING: $\Delta E_{AP_{surf}} < 0$

ABOP: $\Delta E_{AP_{surf}} > 0$

**Only in ISING model
nucleation of a-variant at the surface of c-
variant is energetically favorable.**

L1₀ FePt layers summary III

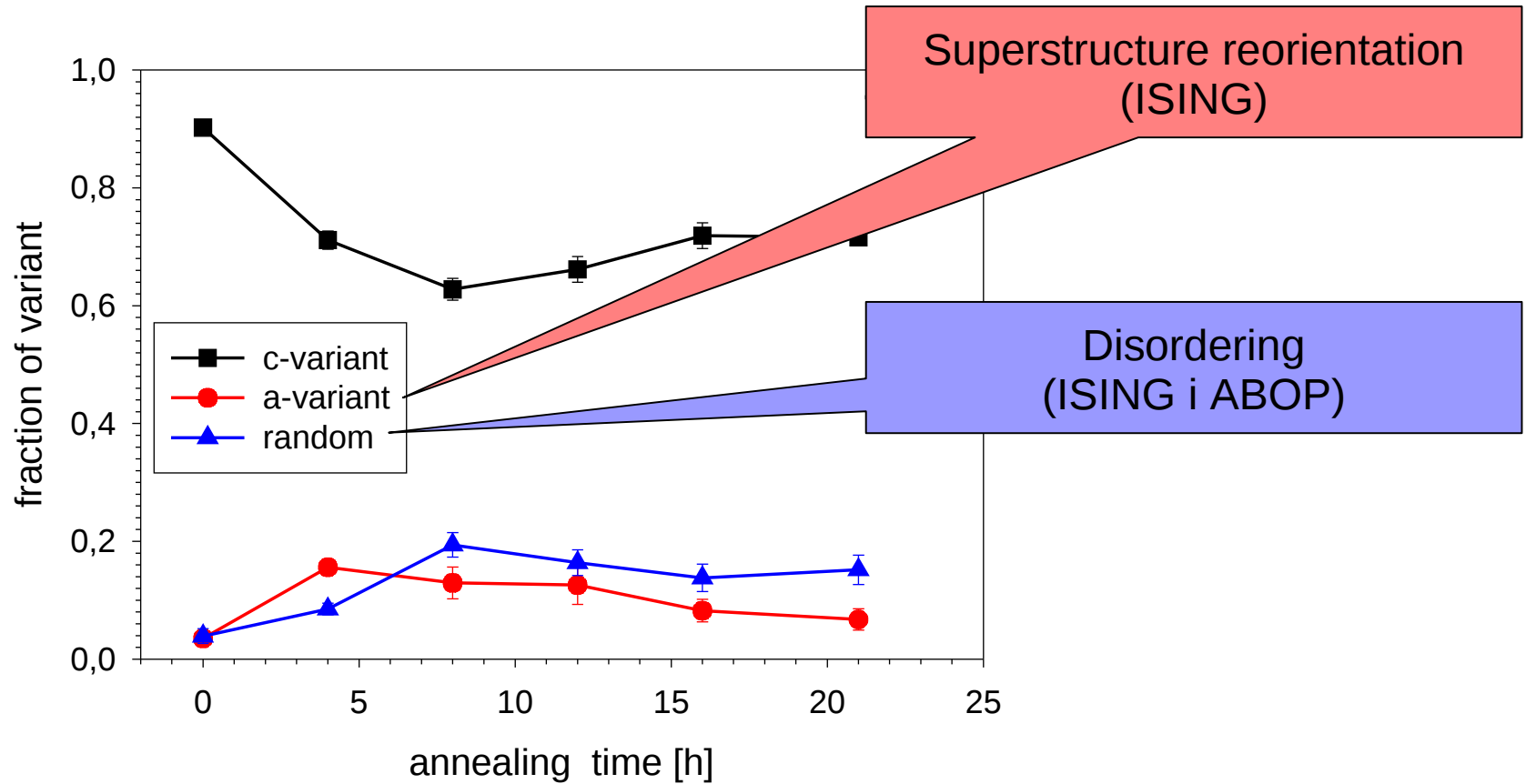
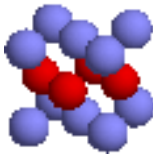


ISING: $\Delta E_{V_{surf}} < 0$

ABOP: $\Delta E_{V_{surf}} < 0$

In ABOP model energy of vacancy migration towards the surface determines the ordering kinetics.

Experimental data instead of conclusion



CEMS-measured evolution of concentration of particular L₁₀ variants in FePt layered sample annealed at 773°C.

Alphard

Atomistic modeling platform

- Dynamic lattice-based simulations
- MC, MD, MS, etc.
- wide range of potentials
- In-depth lattice parameters monitoring and control
- Script-like simulations design



GPL



sourceforge.net/projects/alphard

Thank you for your attention

