

# Beyond the Planck scale

Steven B. Giddings

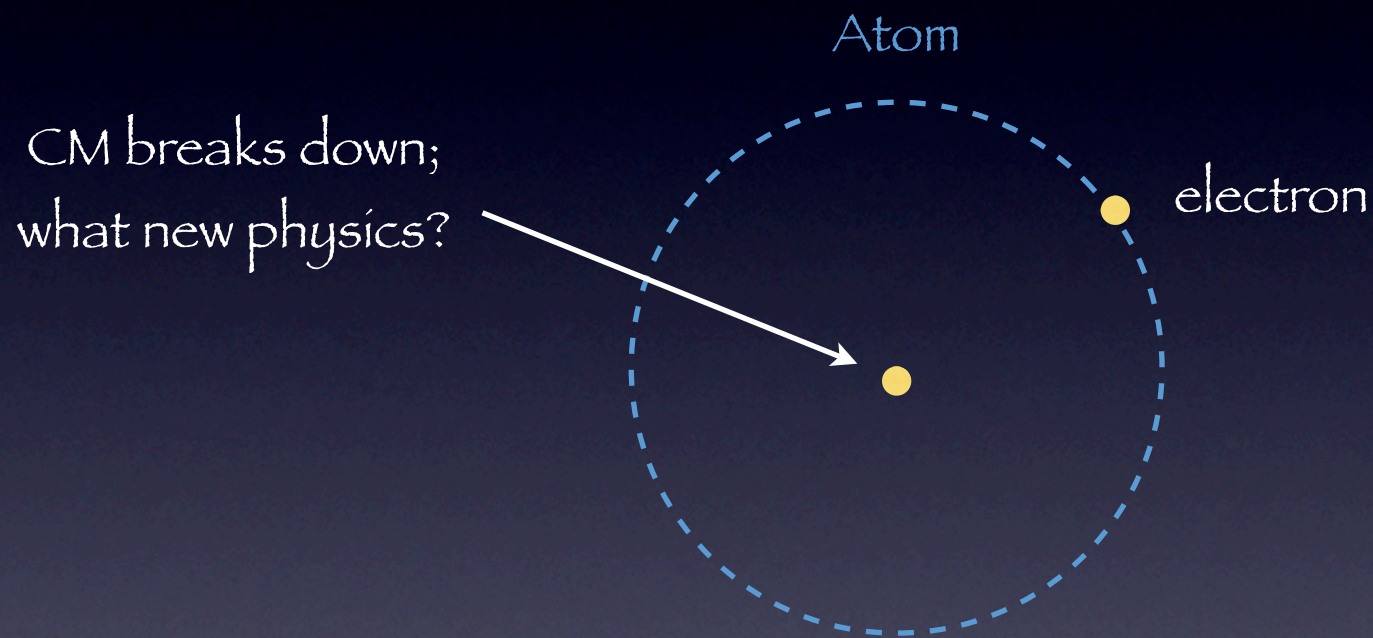
UCSB and CERN

The Planck Scale -- XXV Max Born  
Symposium

Suggestion: focus on the Planck scale  
may be misleading

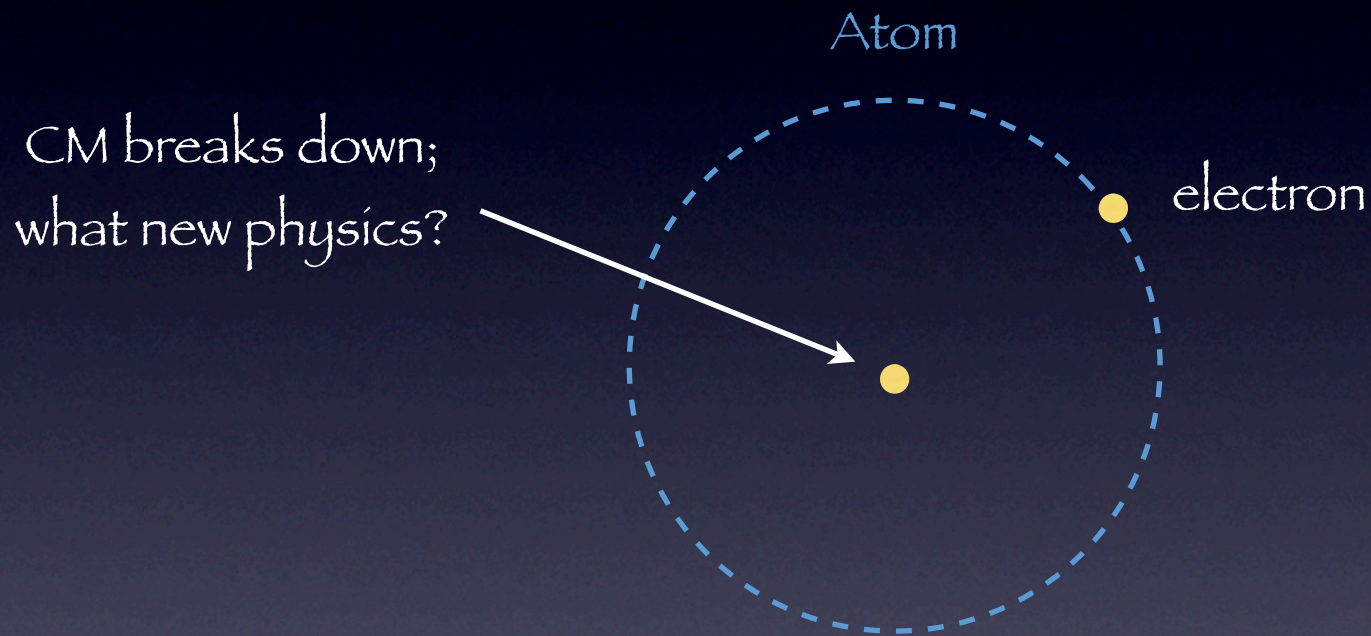
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Experiment guided the resolution:  
1) a different scale ( $a_0$ )      2) new principles (QM)

# Plan:

1) Review arguments

(If you see a better alternative, tell me)

2) Summarize some ongoing work on  
the problem

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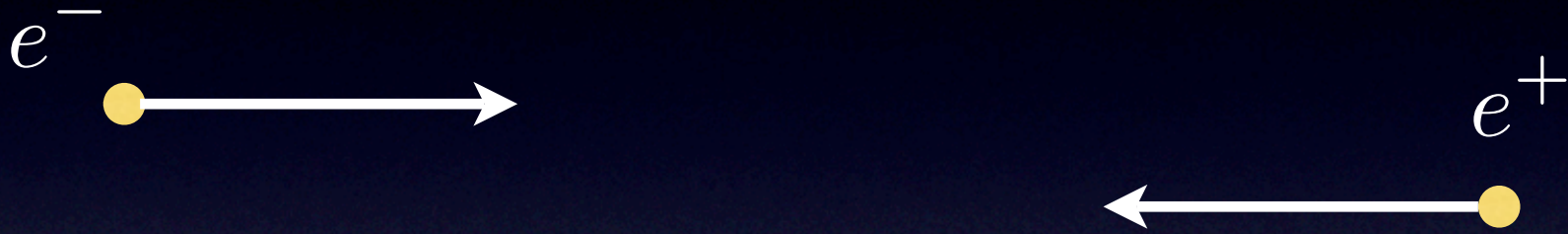
The reason:



Boost to  $E \gg M_p$

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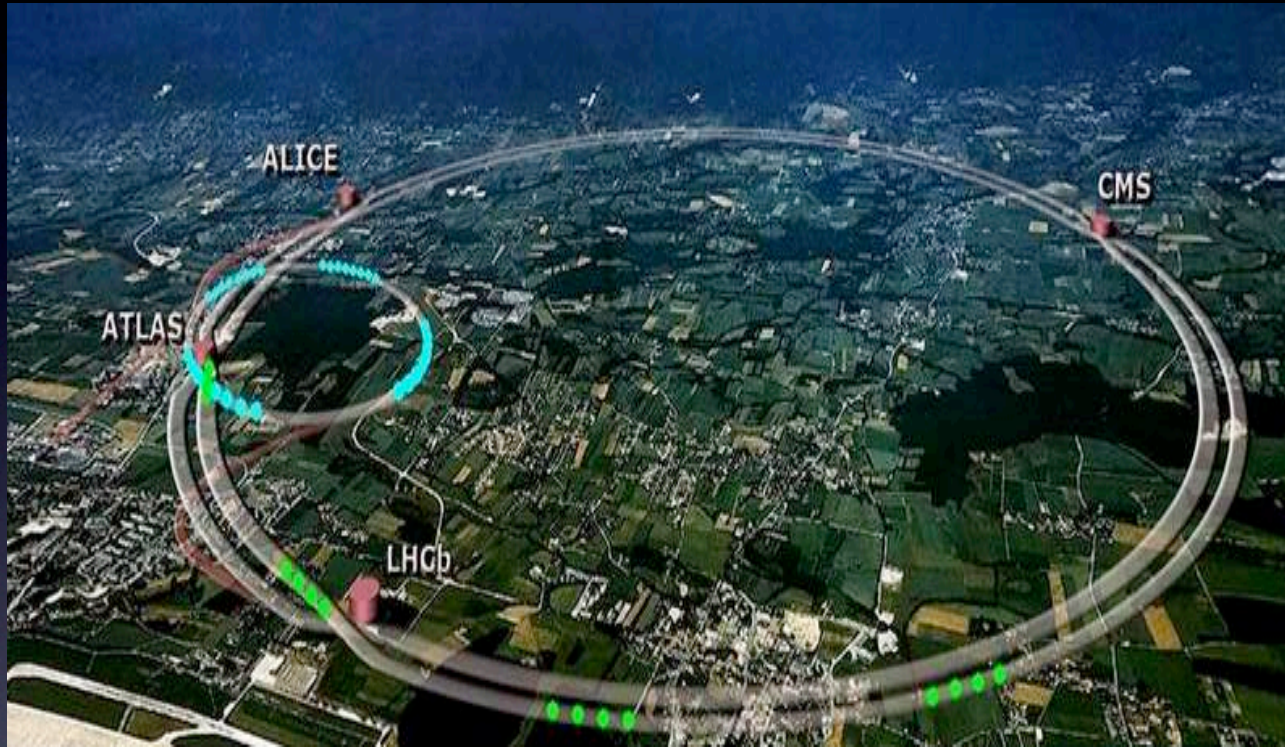
Just need: 1) Lorentz invariance

2) very weak notion of locality

(LI violation might postpone...)



In TeV-scale gravity models, even

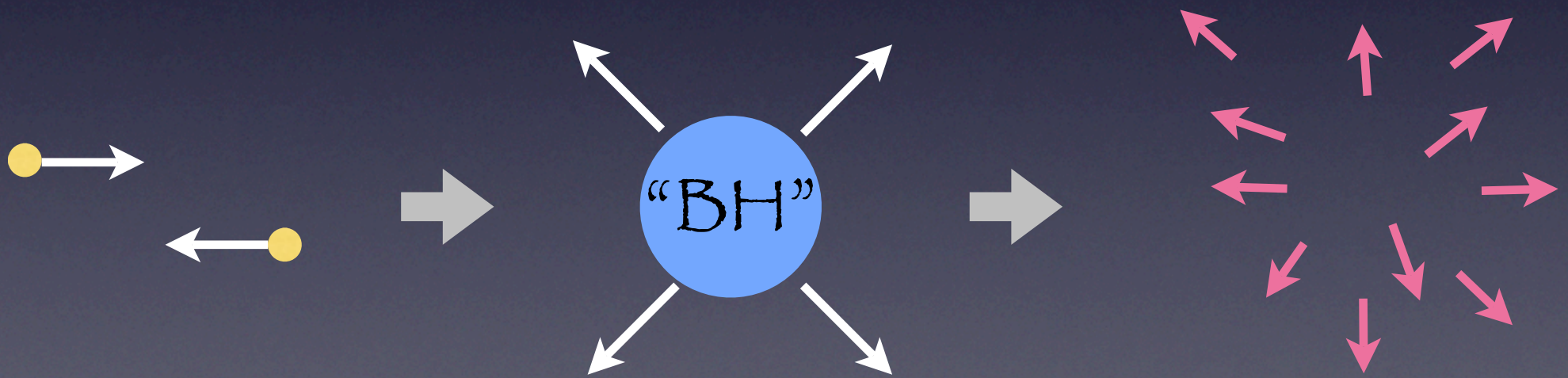


at LHC!

(A review: [arXiv:0709.1107](https://arxiv.org/abs/0709.1107))

# $E \gg M_p$ : dynamics

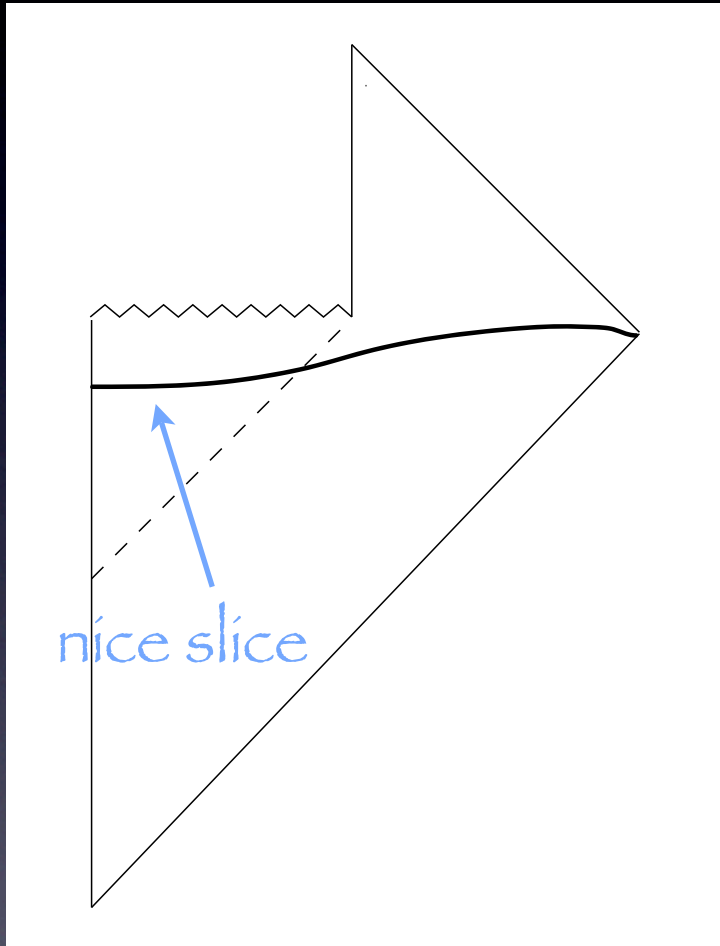
- Control impact parameter  $b$  -- wavepackets
- Large  $E$ :  $\sim$  semiclassical picture
- Classically, produce black hole, + radiation
- Quantum corrections: Hawking radiation



(Indeed,  $\cancel{M}$  doesn't avoid, if form BHs other ways)

So, confront information paradox:

Hawking, updated: nice slice argument



Locality:

$$|\psi_{NS}\rangle \Rightarrow \rho_{out} = \text{Tr}_{in} |\psi_{NS}\rangle \langle \psi_{NS}|$$

$$S_{BH} = -\text{Tr} (\rho_{out} \ln \rho_{out}) \sim A_{BH}$$

$\therefore$  information lost

(Hawking, 1976)

The problem is, QM is remarkably robust:

Banks, Peskin, Susskind (1984):

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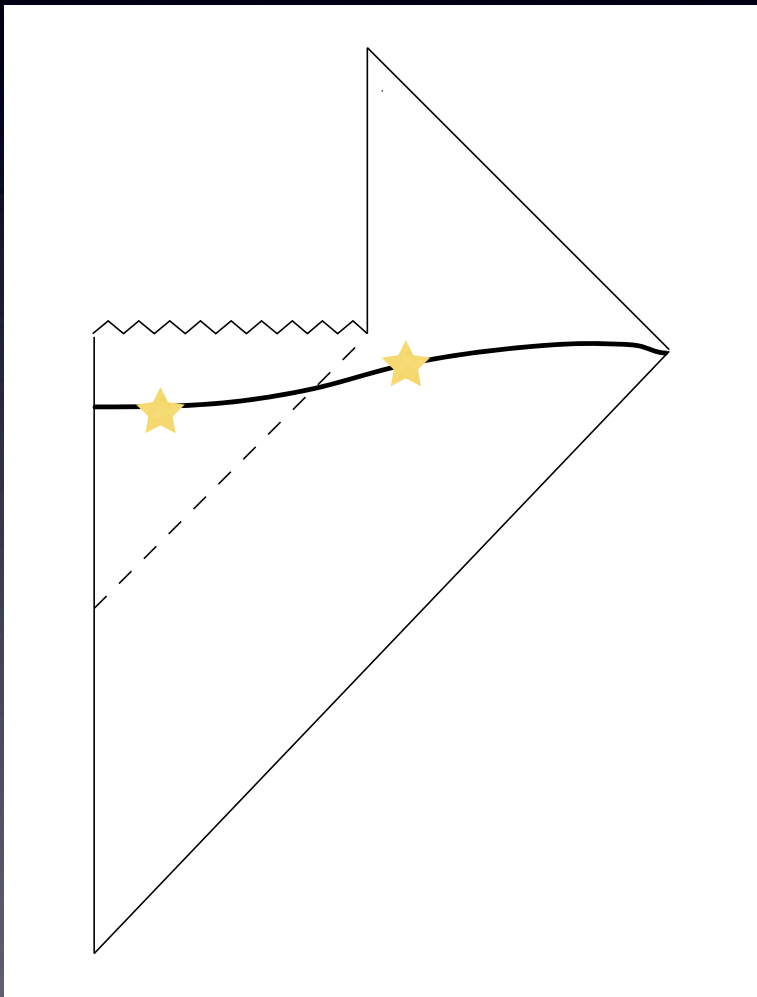
$\therefore$  Let's try to keep unitarity!

Info storage in remnants?      Infinite species

Infinite production instabilities

(See e.g. hep-th/9310101, hep-th/9412159)

So, keeping Lorentz invariance and quantum mechanics apparently tells us to revisit locality:



On scale :

$$R_S \propto (G_D M)^{1/(D-3)}$$

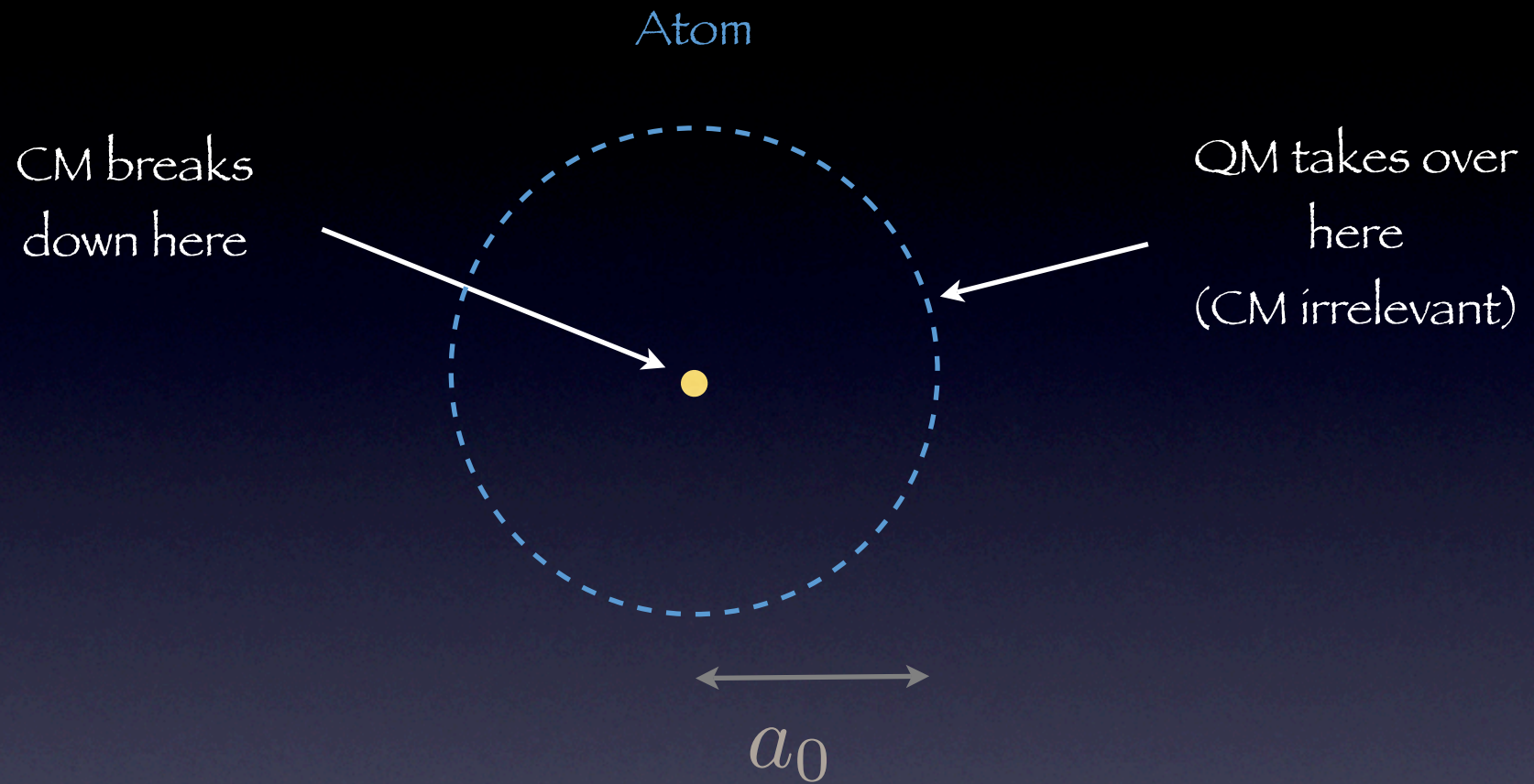
$$\gg \gg \gg l_p$$

By a time:

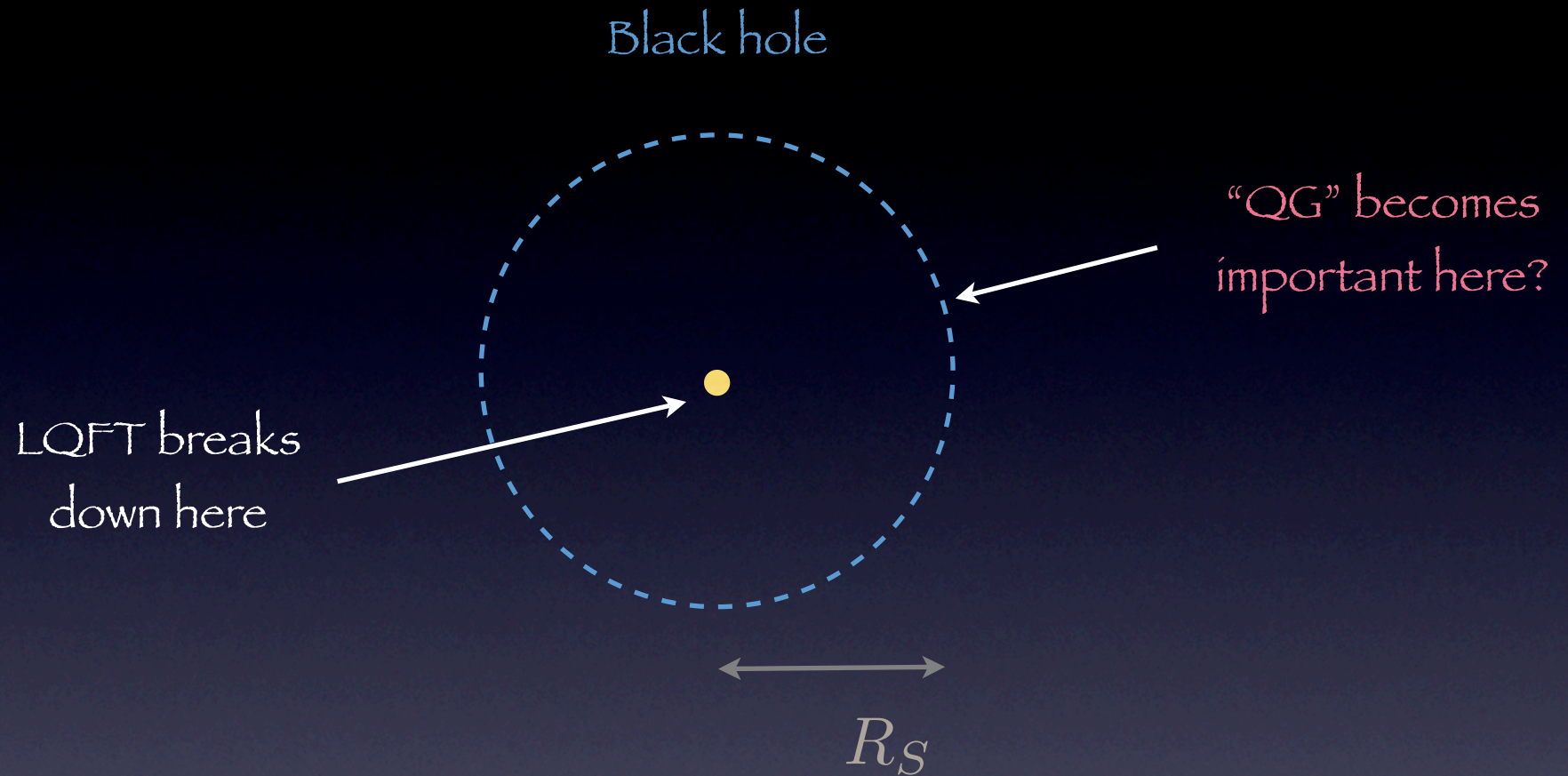
$$\tau \sim R_S S_{BH}$$

(Page, hep-th/9306083)

# The atomic analogy:



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Suggestion: take literally -- new principles at  $R_S$



# What does string theory say?

Hints (?) at a solution: addresses nonrenormalizability  
extendedness/nonlocality  
microstate counting, etc.

Idea: “holography:”

$D$ -dim. grav  $\equiv$   $(D-1)$  non-grav unitary thy  
(AdS/CFT)

But ...

# 1) No apparent role for string extendedness

SBG, hep-th/0604072

SBG, Gross, Maharana, arXiv:0705.1816

“different time scales”

# 2) The problem appears intrinsically nonperturbative



$$1 + \mathcal{O} \left[ \left( \frac{R_S(E)}{b} \right)^{2(D-3)} \right]$$

(unitarity a more critical issue than renormalizability ?)

3) Microstate counting: not far from BPS  
(Schwarzschild)

4) Holographic “duals” don’t clearly contain sufficient  
information

- A test: recover the flat space  $S$ -matrix

Limited progress: Gary, SBG, Penedones arXiv:0903.4437

Potential obstacles: Gary, SBG arXiv:0904.3544

- No understanding of  $\sim$  local observables

(And such strong holography seems possibly overoptimistic)

Whether or not strings the solution ...

## Questions to answer:

1) Where does local QFT fail? Correspondence boundary  
what is wrong with nice slice argument?

2) What is the **mechanism**?

how does it preserve unitarity?

3) What physical/mathematical framework replaces  
QFT, and how might locality emerge from it in  
familiar contexts?

how to preserve consistency/causality?

# Breakdown of classical mechanics:

1) Where fails:  $\Delta x \Delta p = 1$  (~~phase space~~)

(correspondence boundary)

2) Mechanism: wave behavior of matter

classical phase space  $\longrightarrow$  quantum wavefunction

3) Framework: Hilbert space; Schrodinger/  
Heisenberg mechanics

# Some possible proposals for a correspondence boundary for gravity:

planckian curvature:  $\mathcal{R} < M_P^2$

string uncertainty principle:  
(Veneziano/Gross)  $\Delta X \geq \frac{1}{\Delta p} + \alpha' \Delta p$

modified dispersion:  $p < M_p$

} 1 particle

holographic (information)  
bounds:  $S \leq A/4G_N$

multiparticle

dynamical descript.

validity

CM:

$x(t), p(t)$

$$\Delta x \Delta p > 1$$

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QFT  
+GR:

$$\phi_{x,p} \phi_{y,q} |0\rangle$$

(min uncertainty wavepackets)



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“locality bound”

(generalizations: N-particle; dS)

SBG & Lippert;  
hep-th/0605196;  
hep-th/0606146

Correspondingly, mechanism:

“delocalization w.r.t. semiclassical geometry,  
intrinsic to unitary dynamics of nonperturbative  
gravity”

~ “nonlocality principle”

contrast with: extended strings (or branes)

(correspondingly, clear distinction between “string  
uncertainty principle” and the locality bound)

# How do we probe/quantify locality?

- local observables

- high-energy scattering

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Asymptotically flat space:

The gravitational S-matrix

Investigate general properties of scattering,  
consistent with unitary quantum evolution,  
basic features of gravity

e.g: locality  $\longleftrightarrow$  polynomiality?

SBG and Srednicki arXiv:0711.5012

SBG and Porto, WIP

2 → 2 scattering:

PW expansion:

$$T(s, t) = (\text{const}) E^{4-D} \sum_{l=0}^{\infty} (l + \nu) C_l^\nu(\cos \theta) \left[ e^{2i\delta_l(s) - 2\beta_l(s)} - 1 \right]$$

$$\nu = \frac{D-3}{2}$$

A. Can infer features of  $\delta_l, \beta_l$  in “weak gravity” regime (large impact param. -- Born, eikonal)

B. Ansatz for BH region

$$l \lesssim ER_S(E) = L$$

$$\beta_l \approx \frac{S(E, l)}{4}$$

(Bekenstein-Hawking entropy - approx. thermal description)

## Features:

- significant indications, amplitudes not polynomial:

$$T(s, t) \sim e^{s^\alpha t^\beta}$$

plausibly associated w/ lack of usual locality?

(related: viol. of Froissart, eg  $\sigma_{BH} \sim [R_S(E)]^{D-2}$ )

- interesting constraints from crossing

(not “too” nonlocal)



This is “outside” (asymptotic) viewpoint. To discuss “inside,” need local observables

Indeed, locality - QFT:

$$[\mathcal{O}(x), \mathcal{O}(y)] = 0, \quad (x - y)^2 > 0$$

Diff invariance  $\Rightarrow$  None in gravity!

Likely resolution: Relational approach:

“proto-local observables”

see: SBG, Marolf, Hartle;

Gary & SBG: 2d, concrete

Basic idea:

$$\mathcal{O} = \int d^4x \sqrt{-g} B(x) O(x)$$
$$\langle B(x) \rangle = b(x)$$

for appropriate background:  $\langle \mathcal{O} \rangle \approx O(x_0)$

localization relative to background

- But:
- localization only approximate
  - must include background/observer

In the inside perspective, can find flaw in nice slice argument, and see where Hawking went wrong?

Some thoughts:  
hep-th/0606146

Sharp computation of  $S_{BH}$   
requires fine-grained, local  $|\psi\rangle_{NS}$

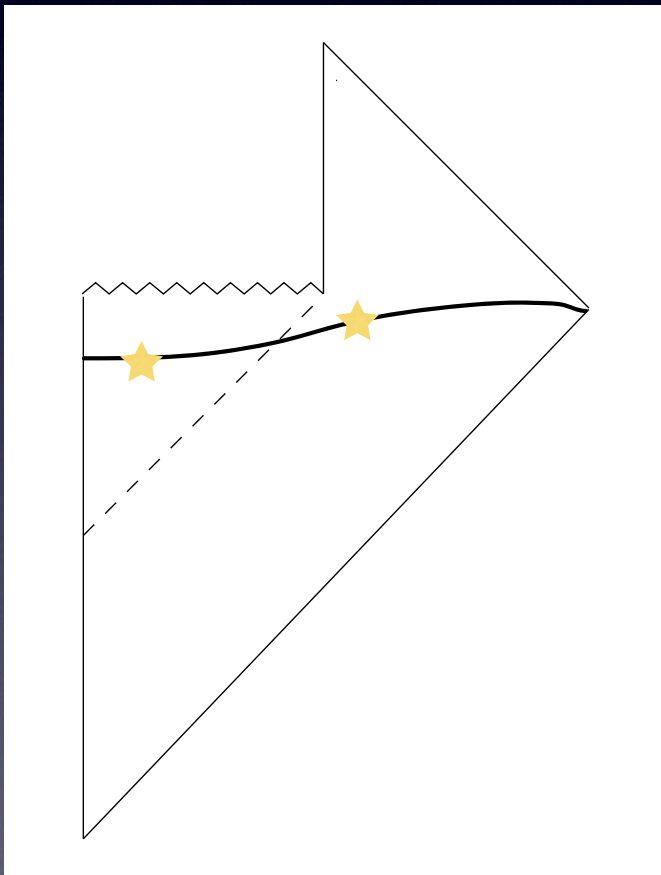
Two potential obstacles:

1) observ. background  $\Rightarrow$   
large mods. to  $|\psi\rangle_{NS}$

2) backreaction of fluctuations  $\Rightarrow$   
large mods. to  $|\psi\rangle_{NS}$

Both by  $\tau_{Page} \sim R_S S_{BH}$

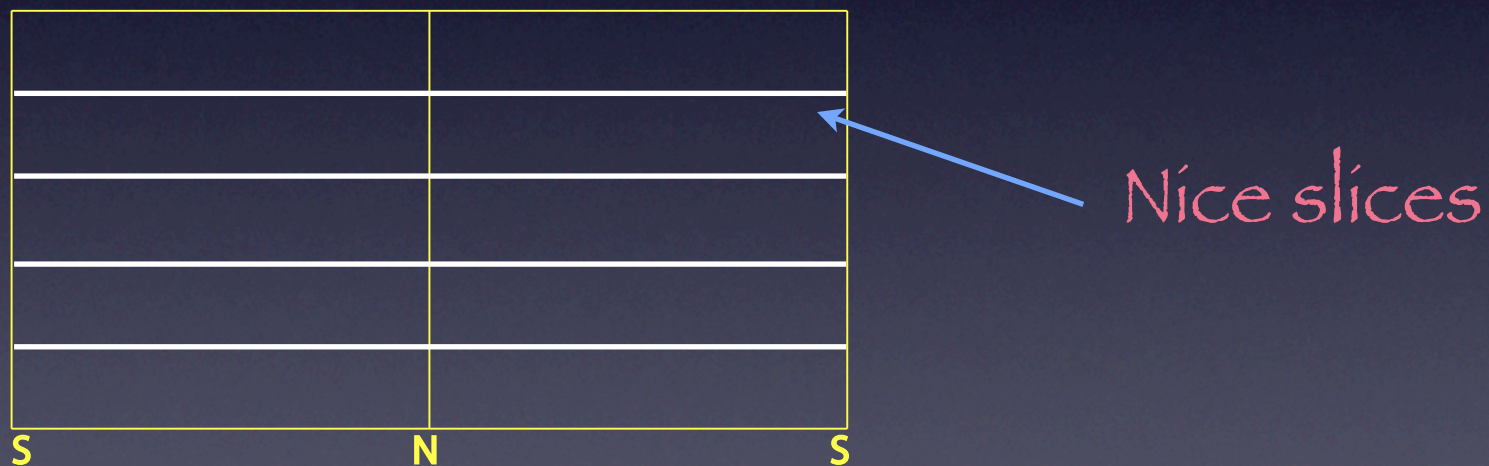
(literal CM/QM analogy may be another out...)



- Apparent signals of perturbative breakdown;  
proposed resolution of information paradox

- Non-pert. completion would be required to  
describe information “relay” / restore unitarity  
but, a clue ...

- Interestingly, there are parallel arguments in dS,



suggesting LQFT incomplete after  $\tau \sim R_{dS} S_{dS}$

(Likely related argument: Arkani-Hamed et al arXiv:0704.1814)

In general, expect similar considerations to possibly be important in cosmology

Work w/ Marolf on dS, etc. arXiv:0705.1178, and WIP x2

- More general limitations on local QFT for volumes  $> R_{dS}^4 e^{S_{dS}}$

- Investigation of proto-local observables in dS  
deal w/ constraints, linearization stability

- Measurement for protolocal observables

To sum up, should be probing limits of local quantum field theory description, likely on scales  $\gg l_P$

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How to progress?

(~ How to invent QM w/out experiment?)

One small step: what is a general enough quantum-mechanical framework to incorporate these ideas?

More general than “generalized QM”

arXiv:0711.0757

Thought experiments, pursuing a consistent quantum description of

- high energy scattering
- observables
- cosmology

and **eliminating** superfluous concepts



# How can we have a theory w/ features of gravity:

1) Consistent (~causal)

2) Quantum mechanical

3) Nonlocal

4) Nearly-local

} essential tension

(i.e. behaves locally in usual low-energy circumstances)

A highly non-trivial set of conditions to satisfy!

Might this help guide us to such a “Non-Local (but Nearly-Local) Mechanics”?



# Backups

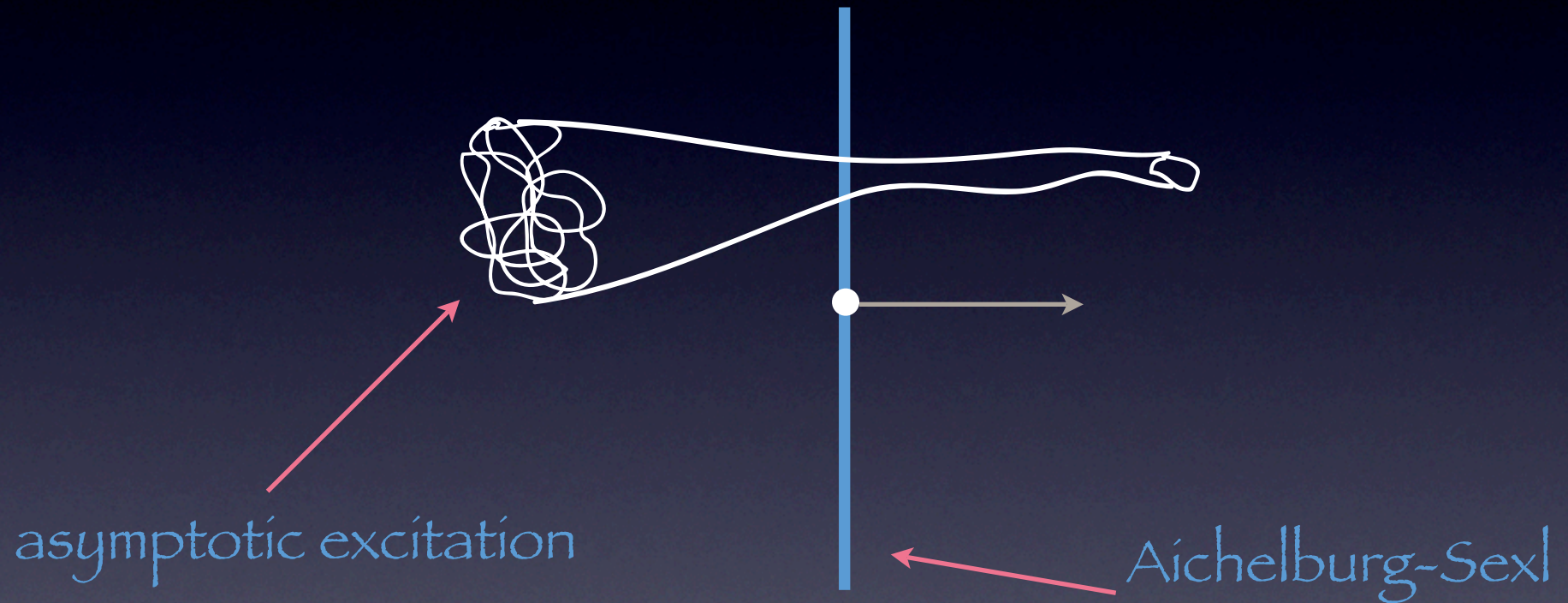
# Tidal string excitation

# Q1: understand diffractive excitation

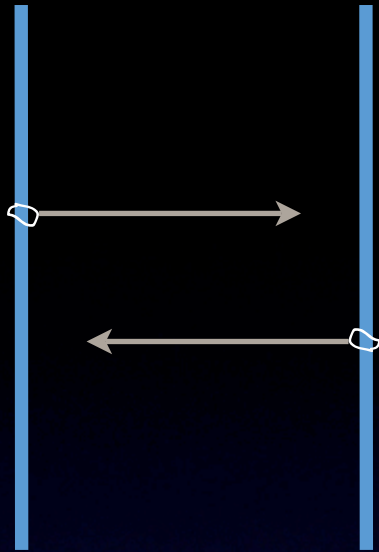
Picture:

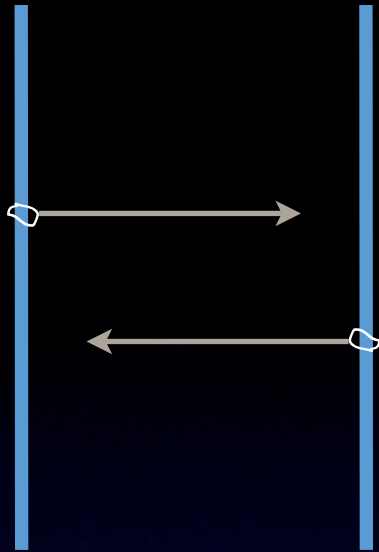
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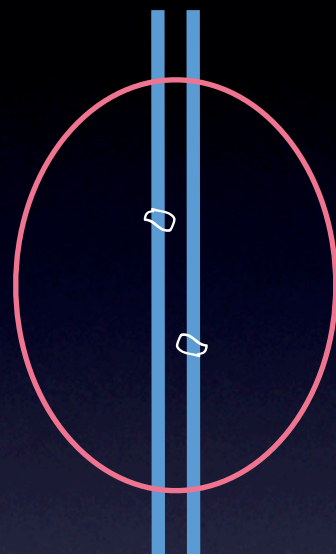
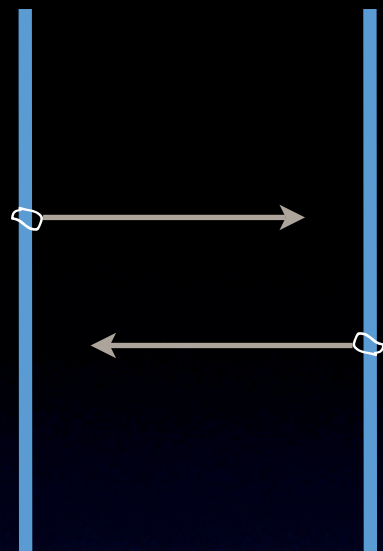
arXiv:0705.1816 w/ Gross and Maharana



“tidal excitation”

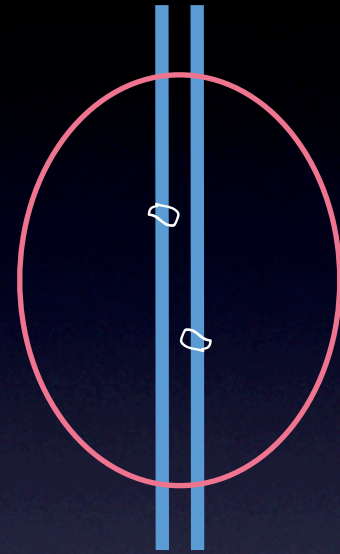
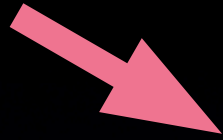
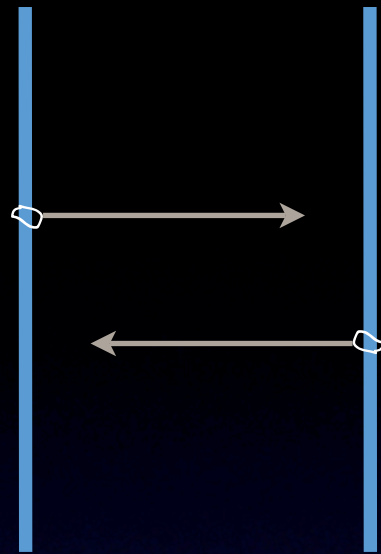




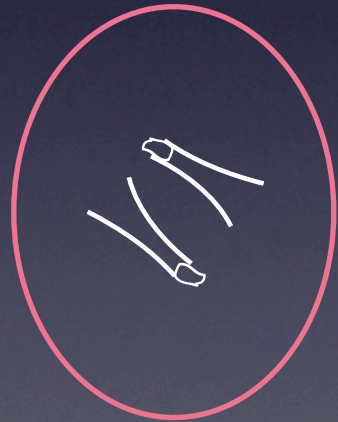


Trapped  
surface





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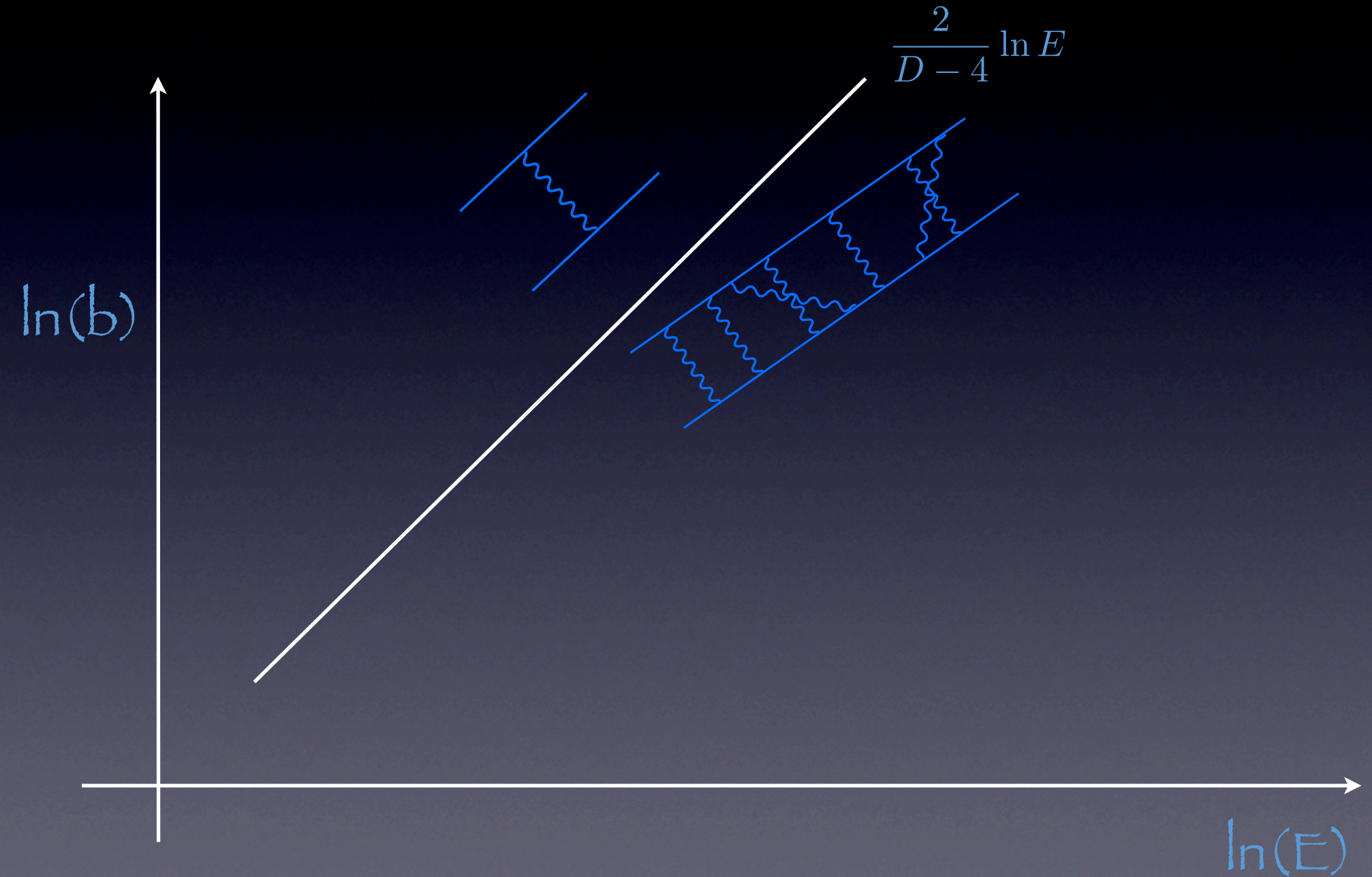
Black hole



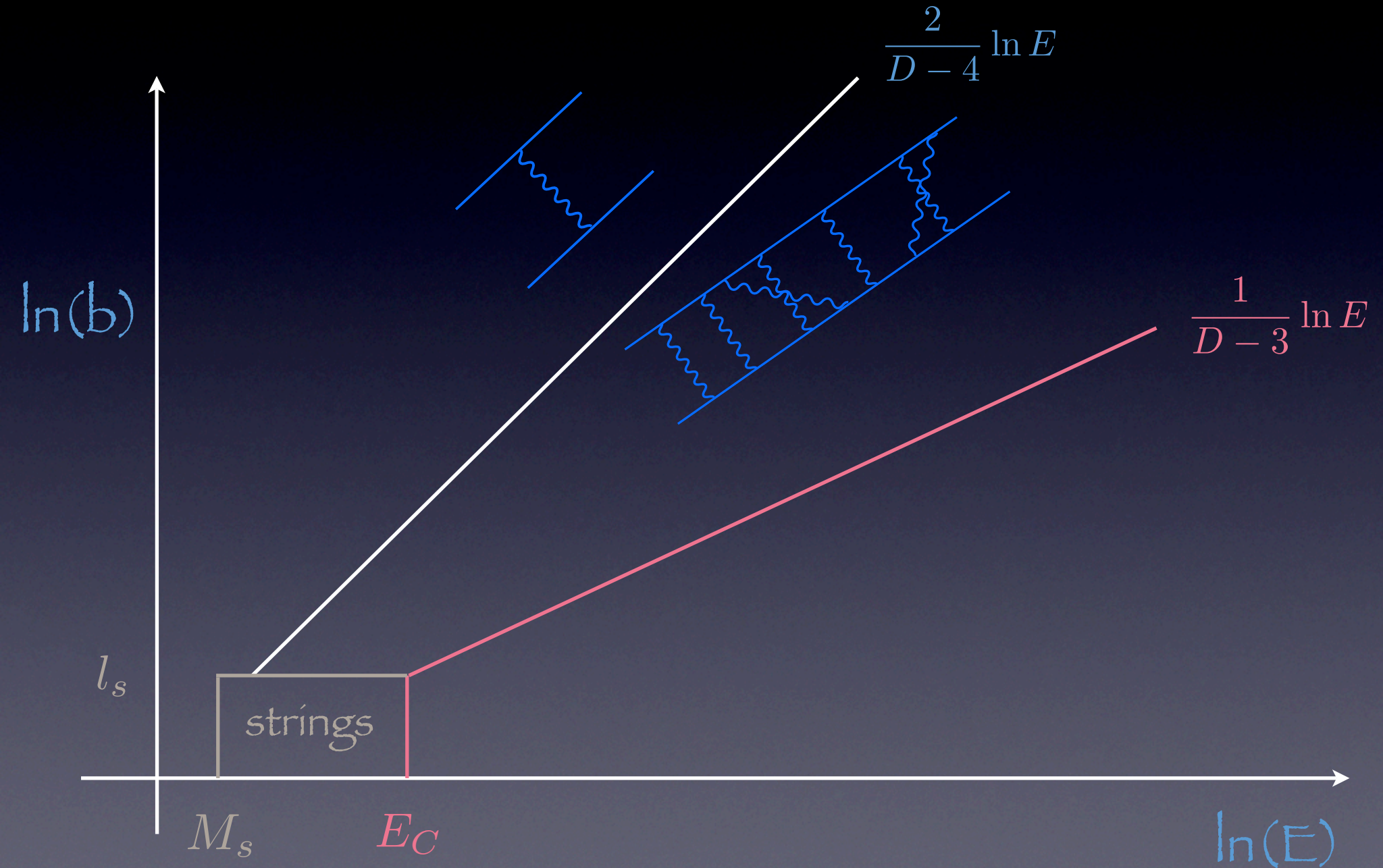
Different timescales  
No role for extendedness?

# Phase diagram

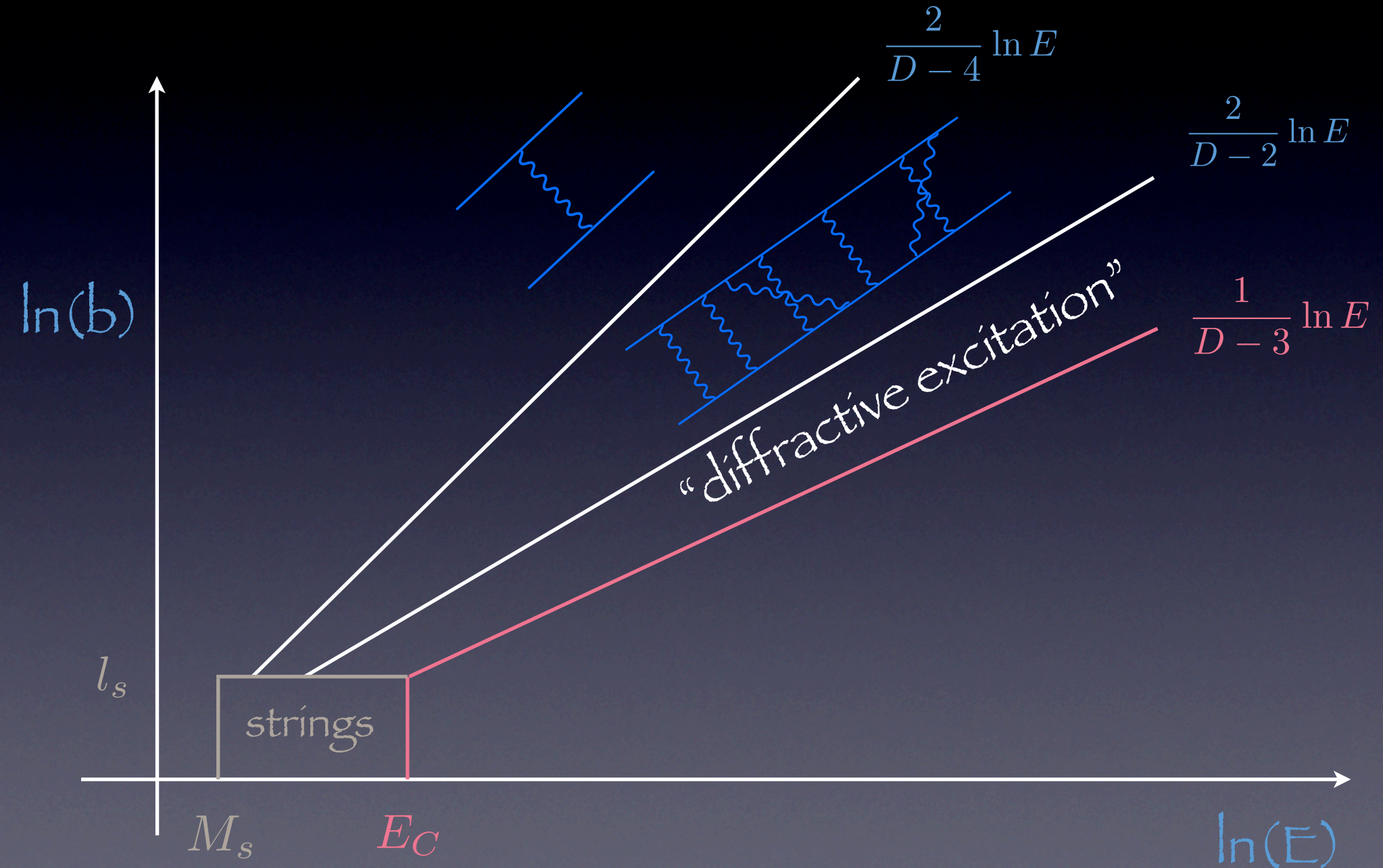
consider strings, or  
more generally

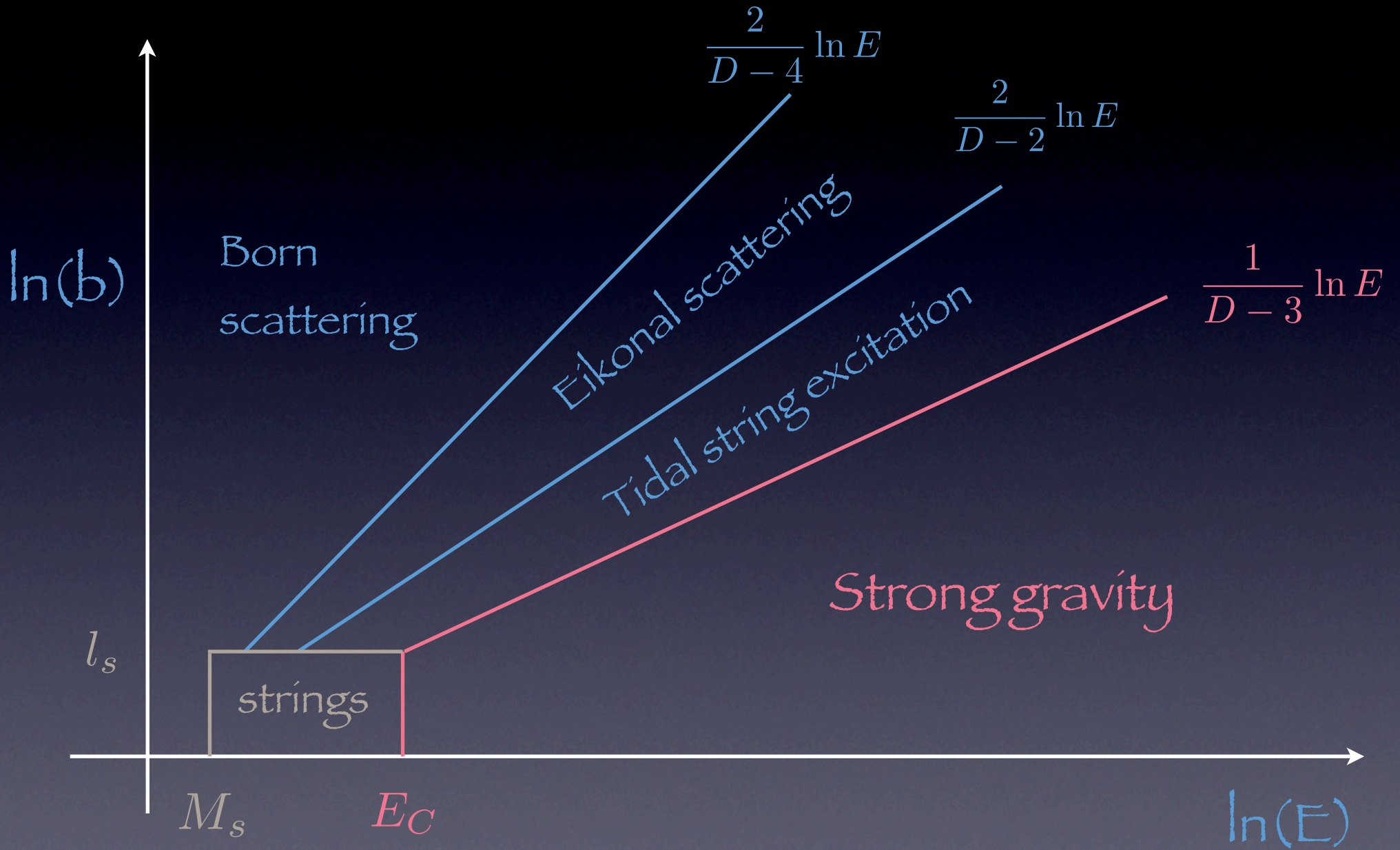


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Locality bd

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de Sitter: see SBG and Marolf, arXiv:0705.1178